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Published in:
Physical Review D

DOI:
10.1103/PhysRevD.106.075022

Publication date:
2022

Document version:
Final published version

Document license:
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Citation for published version (APA):
Cacciapaglia, G., Frandsen, M. T., Huang, W. C., Rosenlyst, M., & Sørensen, P. (2022). Techni-composite Higgs models with symmetric and asymmetric dark matter candidates. *Physical Review D*, 106(7), Article 075022. <https://doi.org/10.1103/PhysRevD.106.075022>

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Techni-composite Higgs models with symmetric and asymmetric dark matter candidates

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(Received 21 December 2021; revised 5 July 2022; accepted 5 October 2022; published 21 October 2022)

We propose a novel class of composite models that feature both a technicolor and a composite Higgs vacuum limit, resulting in an asymmetric dark matter candidate. These techni-composite Higgs models are based on an extended left-right electroweak symmetry with a pseudo-Nambu Goldstone boson Higgs and stable dark matter candidates charged under a global $U(1)_X$ symmetry, connected to the baryon asymmetry at high temperatures via the $SU(2)_R$ sphaleron. We consider, as explicit examples, four-dimensional gauge theories with fermions charged under a new confining gauge group G_{HC} .

DOI: [10.1103/PhysRevD.106.075022](https://doi.org/10.1103/PhysRevD.106.075022)

I. INTRODUCTION

The nature of dark matter (DM) and the origin of its relic density are arguably among the most important open questions in particle physics [1]. The observed baryon asymmetry is another important puzzle in the Standard Model (SM) due to the smallness of CP violation in the Cabibbo-Kobayashi-Maskawa matrix [2]. Furthermore, the measured Higgs boson mass is too heavy to trigger a strong first-order phase transition [3,4], hence failing to realize electroweak baryogenesis. Asymmetric dark matter (ADM) [5], in which only DM particles or antiparticles remain today, may provide an elegant, unified solution to these questions by connecting the baryonic and DM relic densities.

It is tantalizing to draw other connections between baryons and DM. For example, consider the composite nature of baryons, whose mass is generated by strong dynamics. This could also be a property of DM if it

originates from a new strongly interacting sector. A classic example is technicolor (TC) [6,7], where the electroweak symmetry is broken dynamically by a fermion condensate analogous to chiral symmetry breaking in QCD. Within TC, neutral massive bound states whose stability is due to $U(1)_X$ techni-baryon charge are DM candidates [5,8]. The baryon and DM relic densities can share a common asymmetric origin if this $U(1)_X$ global symmetry has an electroweak (EW) anomaly, paralleling that of the baryon number in the SM [9]. This realizes ADM [8] in TC models. In view of the progress at the LHC, the main drawback of TC models is that, in general, there is no simple parametric limit in which an SM-like Higgs is recovered.

One way out consists of engineering a vacuum misalignment of TC into a composite Higgs (CH) model [10–12], which is possible for a subset of TC theories [13,14]. The composite Higgs state now arises as a pseudo-Nambu-Goldstone boson (PNGB) from the spontaneously broken (chiral) global symmetry. Hence, it can be parametrically close to the SM Higgs. However, in CH models the $U(1)_X$ techni-baryon or specie number is either broken or no longer anomalous under the EW sphalerons, thus the link between the baryon and DM asymmetric relic densities is severed (see [15–22] for models with thermal composite DM).

In this work, we propose a new model building avenue where the CH and TC limits are simultaneously present, thus allowing for a successful description of the EW symmetry breaking and ADM. This requires the following:

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- (i) a SM-like composite PNBG Higgs multiplet with custodial symmetry [23];
- (ii) a composite DM candidate, stable due to a $U(1)_X$ symmetry of the strong interactions;
- (iii) an EW anomaly of the $U(1)_X$ symmetry allowing for shared asymmetry of baryons and DM;
- (iv) a suppressed DM thermal relic density.

The first ingredient (i) is a key feature of CH models [10], holographic extra dimensions [12,24], little Higgs [25,26], twin Higgs [27] and elementary Goldstone Higgs models [28]. Extensions of the global symmetries can accommodate (ii); however, these model types typically do not satisfy (ii) and (iii) together.

To realize all four requirements of the techni-composite Higgs scenario, we are led to consider an extended left-right EW sector, with gauged $SU(2)_L \otimes SU(2)_R \otimes U(1)_{Y'}$ symmetry, dynamically broken by the strong dynamics via a left-right coset: $G/H \supset G_L/H_L \otimes G_R/H_R$. The left subcoset G_L/H_L is pinned in a CH direction by appropriate interactions, while the right subcoset G_R/H_R is in the TC vacuum with an unbroken global $U(1)_X$. This symmetry is anomalous under $SU(2)_R$, and the lightest composite state carrying X -charge plays the role of ADM. Imposing the requirements (i)–(iv) also constrains nontrivially the form of the operators that generate the SM-fermion masses. Note that the interplay between TC and CH limits was used in Ref. [29], where the TC vacuum is only present at high temperatures. In our paradigm, the two limits coexist at all temperatures.

II. HYPERCOLOR GAUGE GROUPS WITH DM CANDIDATES AND REALISTIC SM FERMION MASS SPECTRA

For concreteness, we consider four-dimensional gauge theories with a single strongly interacting hypercolor (HC) gauge group G_{HC} , with hyperfermions that generate the global symmetry breaking via condensation. For models with a single fermionic representation, the symmetry breaking patterns are known [30,31]: Given N Weyl spinors transforming as the HC \mathcal{R} representation, the three possible classes of vacuum cosets are $SU(N)/SO(N)$ for real \mathcal{R} , $SU(N)/\text{Sp}(N)$ for pseudoreal \mathcal{R} and $SU(N) \otimes SU(N) \otimes U(1)/SU(N) \otimes U(1)$ for complex \mathcal{R} [32]. The minimal CH cosets that fulfil requirement (i), within these three classes, contain $N = 5$ in the real case [11], $N = 4$ in both the pseudoreal [33] and the complex cases [16]. In terms of PNBG spectrum, the pseudoreal case is the most minimal, with only five states. Similarly, the minimal TC cosets that fulfil the requirements (ii)–(iv) contain $N = 4$ in the real case [34–37], $N = 4$ in the pseudoreal [38] and $N = 2$ in the complex one [10]. In the first two, the ADM candidates are PNBGs, while in the complex case it is a baryon [10].

To realize our scenario, we need to introduce two sets $\mathbb{S}_{L,R}$ of hyperfermions, charged under $SU(2)_{L,R}$, respectively. The representations $\mathcal{R}_{L,R}$ may be different or

TABLE I. Fermion field content and their charges of the techni-composite Higgs template models with the full left-right gauge symmetry. All groups are gauged except for $U(1)_X$, which is a global symmetry in the R sector responsible for dark matter stability.

	G_{HC}	$SU(3)_{\text{QCD}}$	$SU(2)_L$	$SU(2)_R$	$U(1)_{Y'}$	$U(1)_X$
(U, D)	\mathcal{R}_L	1	\square	1	0	0
\tilde{U}	\mathcal{R}_L	1	1	1	-1/2	0
\tilde{D}	\mathcal{R}_L	1	1	1	+1/2	0
(C, S)	\mathcal{R}_R	1	1	\square	0	+1
\tilde{C}	\mathcal{R}_R	1	1	1	-1/2	-1
\tilde{S}	\mathcal{R}_R	1	1	1	+1/2	-1
$q_{L,i}$	1	\square	\square	1	+1/6	0
$q_{R,i}$	1	\square	1	\square	+1/6	0
$l_{L,i}$	1	1	\square	1	-1/2	0
$l_{R,i}$	1	1	1	\square	-1/2	0

identical, and they determine the resulting coset structure. We will assume that the pattern of the L and R cosets are the same as above even when the two representations are different, while for $\mathcal{R}_L \equiv \mathcal{R}_R$ the coset is enlarged. The strong G_{HC} interactions produce condensates of the $\mathbb{S}_{L,R}$ fermions at scales $f_{L,R}$, which are of similar size. Hence, the breaking of the EW gauge symmetry occurs as follows:

$$SU(2)_L \otimes SU(2)_R \otimes U(1)_{Y'} \xrightarrow{f_R} SU(2)_L \otimes U(1)_Y \xrightarrow{f_L \sin \theta_L = v_{\text{EW}}} U(1)_{\text{EM}}, \quad (1)$$

where the hierarchy between the EW scale v_{EW} and the compositeness scale $f_L \sim f_R$ is generated in the \mathbb{S}_L sector and is parametrized by a (small) angle θ_L .

The most minimal choice for the \mathbb{S}_L sector consists in four Weyl spinors Q_L , arranged in one $SU(2)_L$ doublet (U, D) and two singlets \tilde{U} and \tilde{D} , transforming as a pseudoreal representation \mathcal{R}_L of G_{HC} and as a fundamental of a global $G_L = SU(4)_L$. The minimal L coset will, therefore, contain the longitudinal components of the W^\pm and Z bosons, a Higgs candidate, and a singlet η . We will focus on this scenario in the following, as shown in Table I.¹ The minimal \mathbb{S}_R also contains four Weyl spinors Q_R , arranged in an $SU(2)_R$ doublet (C, S) and two singlets \tilde{C} and \tilde{S} . The quantum numbers, together with the $U(1)_X$ charges, are shown in Table I, and are valid for all possible representations \mathcal{R}_R : in the complex case, however, the singlets \tilde{C} and \tilde{S} transform as the conjugate \mathcal{R}_R^* , while $U(1)_X$ is the techni-baryon number. In the pseudoreal case, the coset is $SU(4)_R/\text{Sp}(4)_R$ and, besides the longitudinal modes of the W_R^\pm and Z_R bosons, the spectrum contains

¹The same gauge charge assignment can be used for a complex \mathcal{R}_L , at the price of including right-handed hyperfermions with the same quantum numbers. For real \mathcal{R}_L one would need two $SU(2)_L$ doublets with opposite $U(1)_{Y'}$ charges and a neutral singlet, thus five Weyl spinors in total.

a complex neutral PNBG carrying X -charge. In the real case, the coset $SU(4)_R/SO(4)_R$ contains a complex neutral PNBG and two charged ones carrying X -charge. In the complex case, the coset $SU(2)_{R1} \otimes SU(2)_{R2} \otimes U(1)_X/SU(2)_{VR} \otimes U(1)_X$ does not contain PNBGs carrying X -charge, so the DM candidate is played by a baryon-like state. In all cases, the $U(1)_X$ symmetry has a gauge anomaly with respect to the $SU(2)_R \otimes U(1)_{Y'}$ symmetry. Note that, if $\mathcal{R}_L \neq \mathcal{R}_R$, there exists a global $U(1)_\Theta$ symmetry under which both sets of hyperfermions are charged, which is spontaneously broken by the condensates and generates a light singlet PNBG, along the lines of Refs. [39,40]. Finally, if $\mathcal{R}_L = \mathcal{R}_R \equiv \mathcal{R}$, the coset is enhanced: for pseudoreal \mathcal{R} , the coset is $SU(8)/Sp(8)$; for real \mathcal{R} , the minimal case is $SU(9)/SO(9)$; for complex \mathcal{R} , we have $SU(6)_1 \otimes SU(6)_2 \otimes U(1)_{TB}/SU(6)_V \otimes U(1)_{TB}$, where the $U(1)_X$ in Table I is a linear combination of $U(1)_{TB}$ and a $U(1)$ factor inside $SU(6)_V$.

The remaining important ingredient for model building is the list of operators that generate the SM-fermion masses. The operators play an important role in determining the vacuum alignment in both L and R sectors, particularly via the top mass [41]. To connect the $U(1)_X$ anomaly to the baryon number via $SU(2)_R$, we require that the right-handed SM fermions transform as doublets, as shown in the bottom rows of Table I. The operators that generate the fermion masses, therefore, appear as 6-fermion operators with the generic structure $Q_L Q_L Q_R Q_R \psi_L \psi_R$. For instance, for the top quark

$$\frac{\xi_t}{\Lambda_t^5} (Q_L^T P_L Q_L) (Q_R^T P_R Q_R) q_{L,3} q_{R,3} + \text{H.c.}, \quad (2)$$

where P_L and P_R are two-index matrices in the G_L and G_R space, respectively, selecting the appropriate combinations of the hyperfermions that ensure gauge invariance and couple the top fields with the components that acquire a nonzero condensate. As such, $P_{L,R}$ transform as doublets of $SU(2)_{L,R}$, respectively. Similar operators can be added for all SM fermions. Note also that, for complex $\mathcal{R}_{L,R}$, it suffices to replace $Q_{L,R}^T$ by the conjugate hyperfermions. Dangerous flavor changing neutral currents (FCNCs) from those operators are suppressed by kinematic reasons due to the fact that those vertices contain six fermions compared to only four for traditional ‘‘extended technicolor’’ type operators [42] suffering from FCNCs. We also remark that the operator in Eq. (2), reminiscent of the mass terms in the original TC models [7], can be generated via partial compositeness [43] in models proposed in Refs. [44,45] via operators of the following form:

$$\frac{y_L}{\Lambda_t} q_{L,3} (Q_L^T P_L Q_L \chi_t) + \frac{y_R}{\Lambda_t} q_{R,3} (Q_R^T P_R Q_R \chi_t^\dagger) + \text{H.c.}, \quad (3)$$

where χ_t is a new hyperfermion, transforming in a suitable representation of G_{HC} , and carrying appropriate quantum

numbers under the SM gauge symmetry. Those operators also help avoiding FCNCs and generating a large top mass via enhancement from large anomalous dimensions of the fermionic operators the top couples to. To illustrate the new scenario, in the following we will focus on a specific minimal model, and leave other examples in Appendix B.

The minimal scenario we illustrate here is based on $G_{HC} = Sp(6)_{HC}$ with $\mathcal{R}_L = F$ (fundamental, pseudoreal) and $\mathcal{R}_R = A$ (antisymmetric, real). We will also include masses for the hyperfermions in \mathbb{S}_L , because they help stabilize the CH vacuum [13,46]. The relevant physics can be described below the condensation scale in terms of an effective theory, following the Coleman-Callan-Wess-Zumino prescription [47], and based uniquely on the coset symmetry:

$$\frac{SU(4)_L \times SU(4)_R \times U(1)_\Theta}{Sp(4)_L \times SO(4)_R}, \quad (4)$$

where we identify the PNBG Higgs h , three exact Goldstones eaten by the W_L^\pm and Z_L bosons and the pseudoscalar η in the coset $SU(4)_L/Sp(4)_L$ and the pseudoscalar Θ by the spontaneous breaking of $U(1)_\Theta$. Furthermore, we identify the DM candidate as the neutral and lightest component Π_{CS}^0 of a complex isotriplet in the coset $SU(4)_R/SO(4)_R$, which is stabilized by the unbroken $U(1)_X \subset SO(4)_R$. The additional three Goldstone states in $SU(4)_R/SO(4)_R$ are eaten by the W_R^\pm and Z_R bosons.

At lowest order, the effective Lagrangian has the form

$$\mathcal{L}_{\text{EFT}} = \mathcal{L}_{\chi PT} - V_{\text{eff}}, \quad (5)$$

where the first term corresponds to the usual chiral perturbation theory for the PNBGs, and the second term contains the effective potential generated by loops of the SM fields, namely the EW gauge bosons and the fermions (top). The latter plays a crucial role in determining the vacuum alignment and the gauge symmetry breaking (see Appendix A for details). Furthermore, the global $U(1)_X$ symmetry is part of the global symmetry of the strong sector, and therefore it is not broken by any operators generated by the strong dynamics alone. The only operators that might break the $U(1)_X$ symmetry are the fermion mass operators, but we choose to add a specific set of such operators in Eq. (2) or (3)—defining our model—which do not. Hence in the effective theory, the $U(1)_X$ is preserved to all orders, and therefore the stability of the DM candidate is not ruined.

III. ADM RELIC DENSITY AND COLLIDER BOUNDS ON THE $SU(2)_R$ GAUGE BOSONS

To investigate the asymmetric relic, we analyze the dynamics of the sphalerons associated with the left and right gauge symmetries. The $SU(2)_L \times SU(2)_R$ sphaleron equations, when in equilibrium above $f_{L,R}$, yield chemical potential equations of the form

$$\begin{aligned}
(\mu_{uL,i} + 2\mu_{dL,i}) + \mu_{\nu L,i} + \frac{d(\mathcal{R}_L)}{2}(\mu_U + \mu_D) &= 0, \\
(\mu_{uR,i} + 2\mu_{dR,i}) + \mu_{\nu R,i} + \frac{d(\mathcal{R}_R)}{2}(\mu_C + \mu_S) &= 0, \quad (6)
\end{aligned}$$

where sums over the generations are left understood and $d(\mathcal{R})$ is the dimension of representation \mathcal{R} . The labeling of the chemical potentials μ follows Ref. [38]. The alignment of the \mathbb{S}_L sector vacuum also results in the separate equation $\mu_U + \mu_D = 0$. Together with equilibrium conditions from the 6-fermion operators in Eq. (2) and conditions on the relevant charges, these sphaleron processes yield a system that can be solved for the relic density of X -charged states after condensation (see Appendix C for details).

If all three families of SM fermions are gauged under $SU(2)_R$ and all the operators, including both sphalerons, are in equilibrium, then the total $U(1)_X$ asymmetry is zero. However, due to the high scale of $f_{L,R}$ not all families are in equilibrium. A fermion ψ , receiving its mass m_ψ from a Yukawa interaction generated by a 6-fermion operator such as Eq. (2), is in equilibrium at a temperature T if [48,49]

$$2.3 \times 10^4 \times \sqrt{\frac{10 \text{ TeV}}{f}} \frac{m_\psi}{v_{EW}} \gtrsim \left(\frac{f}{T}\right)^{9/2}. \quad (7)$$

The system will have nontrivial solutions if the 6-fermion operators are inefficient for at least one charged fermion but efficient for at least one other charged fermion. By evaluating Eq. (7) at the condensation temperature $T = f$, until which we expect the sphalerons to be active, we find this to be realized for $20 \text{ GeV} \lesssim f \lesssim 3 \times 10^{12} \text{ GeV}$.

In this window, 6-fermion operators are inefficient for at least the electron but efficient for at least the top quark. Solving the set of equilibrium equations under these conditions we find, for both first- and second-order phase transitions, the following ratio:

$$\left|\frac{X}{B}\right| = 2\left(3 + \frac{L}{B}\right), \quad (8)$$

where X , B , and L are the X -charge, lepton and baryon number densities, respectively, and where we leave L and B as free parameters in this work. For second-order phase transitions, Eq. (8) applies even when all 6-fermion operators are inefficient. For first-order phase transitions, the system is underconstrained in absence of efficient 6-fermion operators. The ADM relic density can be expressed in terms of the charge densities as

$$\frac{\Omega_{DM}}{\Omega_B} = \left|\frac{X}{B}\right| \frac{m_{DM}}{2m_p} \sigma\left(\frac{m_{DM}}{2T_F}\right), \quad (9)$$

where T_F is the temperature of the phase transition and $\sigma(x)$ is the Boltzmann suppression factor [38,50].

In absence of Boltzmann suppression ($m_{DM} \ll T_F$), the asymmetry sharing naturally fixes the DM number density to the order of the baryonic number density, so that $\Omega_{DM}/\Omega_B \sim \mathcal{O}(1)$ is found for $m_{DM} \sim \mathcal{O}(m_p)$. The correct relic density $\Omega_{DM}/\Omega_B = 5.36$ [51], therefore, requires either a small DM mass $m_{DM} \ll f_R$, a tuning in $|X/B| \ll 1$, or an exponential suppression in the Boltzmann factor for $T_F \ll m_{DM}$. Another possibility is to allow the decay of the heavy X -charged PNCB into another light stable state [52].

To assure condition (iv), the DM PNCB needs to efficiently annihilate to suppress the thermal component of the relic density. For heavy DM candidates ($m_{DM} > m_{W_R} = g_R f_R/2$), the dominant annihilation channel is in a pair of $SU(2)_R$ gauge bosons, which has a cross section of the form:

$$\begin{aligned}
\langle\sigma v\rangle_{W_R} &= \frac{g_R^4 m_{DM}^2}{32\pi m_{W_R}^4} \sqrt{1 - \frac{m_{W_R}^2}{m_{DM}^2}} \\
&\times \left(1 - \frac{m_{W_R}^2}{m_{DM}^2} + \frac{3 m_{W_R}^4}{4 m_{DM}^4}\right). \quad (10)
\end{aligned}$$

This channel is effective in wiping out the thermal relic if $\langle\sigma v\rangle_{W_R} \gg 3 \times 10^{-26} \text{ cm}^3 \text{ s}^{-1}$ [53], implying

$$m_{DM} \gg 0.073 \text{ TeV} \times \left(\frac{f_R}{\text{TeV}}\right)^2, \quad (11)$$

for $m_{DM} \gg m_{W_R}$. For lighter DM masses, $m_{DM} < m_{W_R}$, the main annihilation mode involves a pair of PNCBs that do not carry X -charges: by studying the potential, we found that the dominant channel involves the $U(1)_\Theta$ PNCB Θ , which can be parametrically lighter than the other PNCBs [40]. The annihilation cross section reads

$$\langle\sigma v\rangle_\Theta = \frac{\lambda_{XX\Theta\Theta}^2}{32\pi m_{DM}^2} \sqrt{1 - \frac{m_\Theta^2}{m_{DM}^2}}, \quad (12)$$

where the quartic coupling is suppressed by the misalignment in the L coset, $\lambda_{XX\Theta\Theta} \sim \lambda_0 (v_{SM}/f_L)^2$. This process can wipe out the thermal density for

$$m_{DM} \ll 0.21 \text{ TeV} \times \left(\frac{\text{TeV}}{f_L}\right)^2 \lambda_0 \quad (13)$$

for $m_\Theta \ll m_{DM}$.

The strongest bound on the compositeness scale comes from direct searches at colliders for W_R , as this state can be produced via Drell-Yann if it couples to the first generation. The most recent CMS bound from dijet resonant searches [54] reads $m_{W_R} \gtrsim 5.2 \text{ TeV}$, which implies for $g_R = g_L$ a bound $f_R \gtrsim 16.4 \text{ TeV}$. If $f_L = f_R$, then this bound also implies a bound on the misalignment in the EW sector (L coset), which we can best express in terms of the fine

tuning parameter $\xi = v_{\text{SM}}^2/f_L^2$ [55]: the W_R searches imply a bound $\xi \lesssim 2.25 \times 10^{-4}$. This is much stronger in this model than the bounds on Higgs compositeness from the Higgs couplings to the SM particles set by the LHC data [56] ($\xi \lesssim 0.1$), and the EW precision measurements [14] ($\xi \lesssim 0.04$). On the contrary, as we expect $m_{\text{DM}} \sim f_R$, the values seem compatible with the limit in Eq. (11). The fine-tuning of one part in 4×10^3 should not discourage the study of this model, as it represents a huge improvement over the fine-tuning in the SM, which for the Higgs mass amounts to one part in 10^{34} against the Planck scale. As already discussed, due to the large DM masses, additional tuning is needed in Eq. (9) to obtain the correct relic density via the asymmetric production.

Another valid possibility consists in tuning the mass of the DM to be $m_{\text{DM}} \ll f_R$. Assuming $|X/B| = \mathcal{O}(1)$ in Eq. (9) (and $T_F \gg m_{\text{DM}}$), saturating the relic density would require $m_{\text{DM}} \approx 1$ GeV. This low mass can be achieved by properly tuning couplings in the effective potential in Eq. (5). A viable implementation is detailed in Appendix A in which the DM candidate is a PNGB and the neutral component of a complex isotriplet. This neutral state can be made light by cancellations among loop contributions to

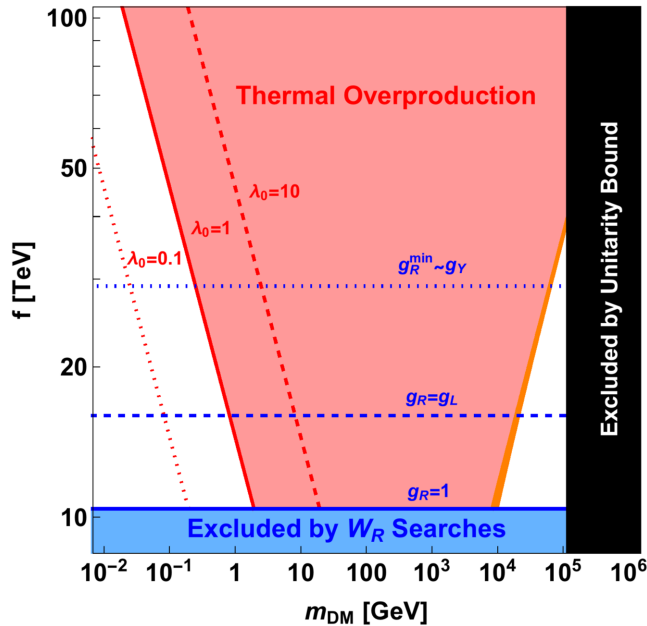


FIG. 1. Constraints on m_{DM} and the compositeness scale $f \equiv f_L = f_R$. The red shaded region is excluded by thermal overproduction, while an upper limit on $m_{\text{DM}} \lesssim 110$ TeV comes from unitarity bounds [58]. The low mass limit of the excluded region depends on λ_0 , and we show three sample values. A lower limit on f comes from direct searches of W_R at colliders, which crucially depends on the value of g_R (we show three sample values: $g_R = 1, g_L, g_Y$, with the last being the minimum allowed value). The high m_{DM} edge of the red region has a mild dependence on g_R , illustrated by the thin orange band, moving to the right for larger g_R .

the mass. This limit is technically natural according to 't Hooft naturalness principle [57] as it reveals the restoration of a global symmetry. The DM candidate is the lightest stable state carrying X -charge and all other PNGB states are accounted for.

IV. CONCLUSION

In this work, we have presented a family of technicomposite Higgs models which employ new strong dynamics to produce both a PNGB Higgs and an asymmetric DM candidate. The key novel ingredient is a left-right symmetry and the contemporary presence of a composite Higgs vacuum in the L sector and a technicolor vacuum in the R sector. An illustrative example of the allowed parameter space is shown in Fig. 1. This shows model independently the main features of technicomposite models: a successful ADM relic density can be obtained for masses above 10 TeV or for masses around the GeV scale. This family of models can thereby naturally explain the observed Higgs mass and DM abundance with a minimum of tuning, although some tuning remains necessary to ensure the correct vacuum alignment and DM mass.

ACKNOWLEDGMENTS

G. C. acknowledges partial support from the Labex-LIO (Lyon Institute of Origins) under Grant No. ANR-10-LABX-66 (Agence Nationale pour la Recherche), and FRAMA (FR3127, Fédération de Recherche “André Marie Ampère”). M. T. F., W. C. H., and M. R. acknowledge partial funding from The Council For Independent Research, Grant No. DFF 6108-00623. The CP3-Origins centre is partially funded by the Danish National Research Foundation, grant number DNRF90. P. S. acknowledges support by the Deutsche Forschungsgemeinschaft under Germany’s Excellence Strategy—EXC 2121 “Quantum Universe”—Grant No. 390833306.

APPENDIX A: EFFECTIVE LAGRANGIAN AND VACUUM ALIGNMENT

We consider the scenario with \mathcal{R}_R real and \mathcal{R}_L pseudoreal of G_{HC} , which applies to the model studied in the main text. To describe the general vacuum alignment in the effective Lagrangian of this scenario, we identify an $\text{SU}(2)_L \times \text{U}(1)_{Y'}$ subgroup in $\text{SU}(4)_L$ by the generators

$$T_{LL}^i = \begin{pmatrix} \sigma_i & 0 \\ 0 & 0 \end{pmatrix}, \quad T_{LY'}^3 = \begin{pmatrix} 0 & 0 \\ 0 & -\sigma_3^T \end{pmatrix}, \quad (\text{A1})$$

and an $\text{SU}(2)_R \times \text{U}(1)_{Y'}$ subgroup in $\text{SU}(4)_R$ by the generators

$$T_{RR}^i = \begin{pmatrix} \sigma_i & 0 \\ 0 & 0 \end{pmatrix}, \quad T_{RY'}^3 = \begin{pmatrix} 0 & 0 \\ 0 & -\sigma_3^T \end{pmatrix}, \quad (\text{A2})$$

where σ_i are the Pauli matrices with $i = 1, 2, 3$. Note that the Y' -charge generator is identified as $Y' \equiv T_{LY'}^3 + T_{RY'}^3$, while the standard hypercharge is given by $Y \equiv T_{LY'}^3 + T_{RR}^3 + T_{RY'}^3$ after the breaking of $SU(2)_R$. Furthermore, $T_{LY'}^3$ and $T_{RY'}^3$ are part of global $SU(2)$ symmetries that define a custodial symmetry in both cosets [23]. This is required in the L coset to reproduce the correct Z/W mass ratio.

The alignment between the extended EW subgroup $SU(2)_L \times SU(2)_R \times U(1)_{Y'}$ and the stability group $Sp(4)_L \times SO(4)_R$ can then be conveniently parametrized by one misalignment angle, θ_L . To do so, we identify the vacua that leave the $SU(2)_L \times U(1)_Y$ symmetry intact, E_L^\pm , and the one breaking $SU(2)_L \times U(1)_Y$ to $U(1)_{EM}$, E_L^B . In the R coset, there is no vacuum that preserves $SU(2)_R \times U(1)_{Y'}$, hence we define the one breaking the gauge group to $U(1)_Y$, E_R^B . They are given in terms of two-index $SU(4)$ matrices as

$$E_L^\pm = \begin{pmatrix} i\sigma_2 & 0 \\ 0 & \pm i\sigma_2 \end{pmatrix}, \quad E_L^B = \begin{pmatrix} 0 & \mathbb{1}_2 \\ -\mathbb{1}_2 & 0 \end{pmatrix},$$

$$E_R^B = \begin{pmatrix} 0 & \mathbb{1}_2 \\ \mathbb{1}_2 & 0 \end{pmatrix}. \quad (\text{A3})$$

Either choice of E_L^\pm is equivalent [33], and in this paper we have chosen E_L^- . The true $SU(4)_L$ vacuum can be written as a linear combination of the above vacua, $E_L(\theta_L) = c_{\theta_L} E_L^- + s_{\theta_L} E_L^B$ (a CH vacuum), while the vacuum of the \mathbb{S}_R sector is $E_R \equiv E_R^B$ (a TC-like vacuum). We use the short-hand notations $s_x \equiv \sin x$, $c_x \equiv \cos x$ and $t_x \equiv \tan x$ throughout.

The Goldstone excitations around the vacuum are then parametrized by

$$\Sigma_L(x) = \exp \left[2\sqrt{2}i \left(\frac{\Pi_L(x)}{f_L} + \frac{\Pi_\Theta(x)}{f_\Theta} \right) \right] E_L(\theta_L),$$

$$\Sigma_R(x) = \exp \left[2\sqrt{2}i \left(\frac{\Pi_R(x)}{f_R} - \frac{\Pi_\Theta(x)}{f_\Theta} \right) \right] E_R, \quad (\text{A4})$$

where the pion matrices Π_x are defined as

$$\Pi_L(x) = \sum_{i=1}^5 \Pi_L^i X_L^i \in G_L/H_L,$$

$$\Pi_R(x) = \sum_{a=1}^9 \Pi_R^a X_R^a \in G_R/H_R,$$

$$\Pi_\Theta(x) = \Theta(x) \frac{\mathbb{1}_4}{4} \in U(1)_\Theta/\emptyset. \quad (\text{A5})$$

The last one encodes the diagonal PNBG state Θ associated with the broken global symmetry group $U(1)_\Theta$, acting on

the two fermion representations and having no gauge anomaly with the HC group. The matrices X_L^i are the θ_L -dependent broken generators of $SU(4)_L$, while X_R^a are the broken generators of $SU(4)_R$. While in general the decay constants are different, for simplicity from now on we will assume $f \equiv f_{L,R} = f_\Theta$.

In the \mathbb{S}_L sector, we identify the wouldbe Higgs boson as $h \equiv \Pi_L^4 \sim c_{\theta_L}(\bar{U}U + \bar{D}D) + s_{\theta_L} \text{Re}U^T C D$ and the singlet PNBG as $\eta \equiv \Pi_L^5 \sim \text{Im}U^T C D$, while the remaining three $\Pi_L^{1,2,3}$ are exact Goldstones eaten by the massive W^\pm and Z . In the \mathbb{S}_R sector, we identify the complex isotriplet scalars,

$$\Pi_{CS}^0 \equiv \frac{\Pi_R^8 + i\Pi_R^9}{\sqrt{2}} \sim C^T C S,$$

$$\Pi_{CC}^+ \equiv \frac{\Pi_R^4 + i\Pi_R^5 + \Pi_R^6 + i\Pi_R^7}{2} \sim C^T C C,$$

$$\Pi_{SS}^- \equiv \frac{\Pi_R^4 + i\Pi_R^5 - \Pi_R^6 - i\Pi_R^7}{2} \sim S^T C S, \quad (\text{A6})$$

where $\Pi_{CS, \overline{CS}}^0$ is identified as the DM candidate. The remaining three, $\Pi_R^{1,2,3}$, are exact Goldstones eaten by the massive W_R^\pm and Z_R . Note that, following Ref. [38], we have used Dirac spinors to indicate the hyperfermions, combining the $SU(2)_{L,R}$ doublet and singlet Weyl spinors.

Below the condensation scale $\Lambda_{HC} \sim 4\pi f$, the effective Lagrangian is given by

$$\mathcal{L}_{\text{eff}} = \mathcal{L}_{\text{kin}} - V_{\text{eff}}. \quad (\text{A7})$$

The kinetic part of the Lagrangian is given by

$$\mathcal{L}_{\text{kin}} = \frac{f^2}{8} \text{Tr}[D_\mu \Sigma_L^\dagger D^\mu \Sigma_L] + \frac{f^2}{8} \text{Tr}[D_\mu \Sigma_R^\dagger D^\mu \Sigma_R], \quad (\text{A8})$$

with

$$D_\mu \Sigma_{L/R} = \partial_\mu \Sigma_{L/R} - i(G_{L/R,\mu} \Sigma_{L/R} + \Sigma_{L/R} G_{L/R,\mu}^T),$$

$$G_{L/R,\mu} = g_{L/R} W_{L/R,\mu}^i T_{L/R}^i + g_{Y'} B_\mu^j T_{LY'/RY'}^j,$$

where $g_{L,R,Y'}$ are the gauge couplings of $SU(2)_L$, $SU(2)_R$ and $U(1)_{Y'}$, respectively. Here the hypercharge coupling is given by $g_Y^{-2} = g_{Y'}^{-2} + g_R^{-2}$. Henceforth, the minimal value g_R can acquire is $g_R^{\text{min}} = g_Y$.

At leading order, each source of symmetry breaking contributes independently to the effective potential in Eq. (A7):

$$V_{\text{eff}} \supset V_{\text{gauge}} + V_{\text{top}} + V_{\text{m}} + V_{\text{B}}. \quad (\text{A9})$$

Here the EW gauge interactions in Eq. (A8) yield the gauge loop contributions to the potential V_{eff} :

$$V_{\text{gauge}} = -C_L f^4 \left\{ g_L^2 \sum_i \text{Tr}[T_{LL}^i \Sigma_L (T_{LL}^i \Sigma_L)^*] + g_{Y'}^2 \text{Tr}[T_{LY'}^3 \Sigma_L (T_{LY'}^3 \Sigma_L)^*] \right\} \\ + C_R f^4 \left\{ g_R^2 \sum_i \text{Tr}[T_{RR}^i \Sigma_R (T_{RR}^i \Sigma_R)^*] + g_{Y'}^2 \text{Tr}[T_{RY'}^3 \Sigma_L (T_{RY'}^3 \Sigma_L)^*] \right\}, \quad (\text{A10})$$

where $C_{L,R}$ encode nonperturbative low energy constants. The top loop contributions arising from the 6-fermion operator

$$\frac{\xi_t}{\Lambda^5} (Q_L^T P_L Q_L) (Q_R^T P_R Q_R) q_{L,3} q_{R,3} + \text{H.c.} \quad (\text{A11})$$

yield the effective potential contribution:

$$V_{\text{top}} = -\frac{1}{4} C_t y_t^2 f^4 \{ |\text{Tr}[P_L \Sigma_L]|^2 |\text{Tr}[P_R \Sigma_R]|^2 \\ + \text{Tr}[P_L \Sigma_L] \text{Tr}[P_R \Sigma_R] \text{Tr}[P_L \Sigma_L^\dagger] \text{Tr}[P_R \Sigma_R^\dagger] \\ + (\text{L} \leftrightarrow \text{R}) \}, \quad (\text{A12})$$

where C_t is a nonperturbative coefficient for the top loop, y_t [proportional to $(\Lambda_{\text{HC}}/\Lambda_t)^5 \xi_t$] is identified by the top Yukawa coupling and the projectors,

$$(P_{L,R}^1)_{ij} = \frac{1}{2} (\delta_{1i} \delta_{3j} \pm \delta_{3i} \delta_{1j}), \\ (P_{L,R}^2)_{ij} = \frac{1}{2} (\delta_{2i} \delta_{4j} \pm \delta_{4i} \delta_{2j}), \quad (\text{A13})$$

select the components of $Q_{L,R}^T Q_{L,R}$ that transform as doublets of $\text{SU}(2)_{L,R}$. Moreover, the explicit hyperfermion bilinear mass terms yield potential contributions:

$$V_m = 2\pi Z_L \text{Tr}[M_L \Sigma_L^\dagger] + \text{H.c.}, \quad (\text{A14})$$

where $M_L = \text{diag}(m_1 \epsilon, -m_2 \epsilon)$ is the mass matrix of the \mathbb{S}_L hyperfermions. Finally, it is relevant to consider possible 4-hyperfermion operators in the \mathbb{S}_R sector of the form $Q_R Q_R Q_R Q_R$, which yield potential contributions [36]:

$$V_B = C_B g_B^2 f^4 \text{Tr}[B \Sigma_R^\dagger B \Sigma_R]. \quad (\text{A15})$$

The coefficients $C_{L,R}$, C_t , Z_L , and C_B in Eqs. (A10)–(A15) are $\mathcal{O}(1)$ form factors that can be computed on the lattice [59]. At leading order, the effective potential for the misalignment angle is given by

$$V_{\text{eff}}^0 = -8\pi f^3 Z_L m_{UD} c_{\theta_L} - f^4 C_L \tilde{g}_L^2 c_{\theta_L}^2 - f^4 C_t y_t^2 s_{\theta_L}^2, \quad (\text{A16})$$

where $m_{UD} \equiv m_1 + m_2$ and $\tilde{g}_L^2 \equiv (3g_L^2 + g_{Y'}^2)/2$. By minimizing the above potential, $\partial_{\theta_L} V_{\text{eff}}^0 = 0$, we obtain

$$c_{\theta_L} = \frac{4\pi Z_L m_{UD}}{f(C_t y_t^2 - C_L \tilde{g}_L^2)}, \quad (\text{A17})$$

where the G_L/H_L part of the vacuum is aligned in a composite Higgs direction ($0 < c_{\theta_L} < 1$), while the G_R/H_R part of the vacuum remains in a TC direction. The conditions for this vacuum alignment to be a stable minimum in the presence of these terms are $\partial_{\theta_L} V_{\text{eff}}^0 > 0$ and that all the squared masses of the PNBGs are positive. However, the condition $\partial_{\theta_L} V_{\text{eff}}^0 > 0$ is fulfilled by requiring $m_h^2 > 0$ due to the fact that $\partial_{\theta_L} V_{\text{eff}}^0 = f^2 m_h^2$. Therefore, we need that all the PNBGs have positive squared masses. The Higgs and η masses are

$$m_h^2 = 2(C_t y_t^2 - C_L \tilde{g}_L^2) v_{\text{EW}}^2, \quad m_\eta^2 = m_h^2 / s_{\theta_L}^2, \quad (\text{A18})$$

while the masses of the complex isotriplet composite scalars, $\Pi_{CS,\overline{CS}}^0$, Π_{CC}^\pm , Π_{SS}^\pm , in the \mathbb{S}_R sector are

$$m_{\Pi_{CS}^0}^2 = 2(C_B g_B^2 - C_R \tilde{g}_R^2 + C_t y_t^2 s_{\theta_L}^2) f^2, \\ m_{\Pi_{CC}^\pm}^2 = m_{\Pi_{SS}^\pm}^2 = m_{\Pi_{CS}^0}^2 + 2C_R g_{Y'}^2 f^2, \quad (\text{A19})$$

where $\tilde{g}_R^2 \equiv (-g_R^2 + g_{Y'}^2)/2$. To obtain a stable vacuum, we therefore need $m_h^2 > 0$ and $m_{\Pi_{CS}^0}^2 > 0$. Following the common lore that the top loops tend to break the electroweak symmetry while gauge loops preserve it, we assume that the form factors $C_{L,R,i} > 0$. Hence, the masses squared are always positive, as long as the top loops dominate, as expected as the Yukawa coupling is larger than the gauge ones. Furthermore, in the R coset, we find that $\tilde{g}_R^2 \geq 0$ for $g_R \geq \sqrt{2} g_Y$, while it becomes positive for $g_Y < g_R < \sqrt{2} g_Y$. In the latter range, it tends to cancel the contribution of the top. As $m_{\Pi_{CS}^0}^2 = m_{\text{DM}}^2$, the magnitude of the dark matter candidate mass crucially depends on the value of these coefficients. In general, the first Eq. (A19) implies that the DM mass is of the order of the PNBG decays constants, i.e., $m_{\text{DM}} \sim f$. Small masses, of the order of GeV, could be obtained if a tuned cancellation is enacted. This could happen if the gauge contribution is large and positive, for $g_R \gtrsim g_Y$, or for $C_B < 0$.

As discussed in the main text, for light DM mass the annihilation is dominantly into the light PNBG associated with the $\text{U}(1)_\Theta$ symmetry. If either of the vectorlike masses m_1 or m_2 are vanishing, then the PNBG Θ state mixes with the \mathbb{S}_L PNBG η state, resulting in that the mass

eigenstate $\tilde{\Theta}$, consisting mostly of Θ , is massless while $\tilde{\eta}$ has a mass of order f :

$$m_{\tilde{\Theta}}^2 = 0, \quad m_{\tilde{\eta}}^2 = \frac{1}{4} \frac{m_h^2}{s_{\theta_L}^2} (5 + c_{2\theta_L}) \approx \frac{3m_h^2}{2s_{\theta_L}^2}. \quad (\text{A20})$$

However, the $\tilde{\Theta}$ state can achieve a small mass from its mixing with a Θ' state corresponding to the U(1) symmetry which is quantum anomalous. In addition, the mass of Θ' is generated by instanton effects related to the U(1) anomaly [40].

Thus, for DM masses below the W_R mass, the dominant annihilation channel is $\Pi_X \bar{\Pi}_X \rightarrow \tilde{\Theta} \tilde{\Theta}$ with the coupling $\lambda_{XX\tilde{\Theta}\tilde{\Theta}}$ given by

$$\mathcal{L}_{\text{eff}} \supset \lambda_{XX\tilde{\Theta}\tilde{\Theta}} \Pi_{CS}^0 \Pi_{CS}^0 \tilde{\Theta} \tilde{\Theta} \quad (\text{A21})$$

with

$$\begin{aligned} \lambda_{XX\tilde{\Theta}\tilde{\Theta}} &= 4C_t y_t^2 s_{\theta_L}^2 \frac{c_{\theta_L}}{\sqrt{2+c_{\theta_L}^2}} \approx \frac{4}{\sqrt{3}} C_t y_t^2 \left(\frac{v_{\text{EW}}}{f} \right)^2 \\ &\equiv \lambda_0 \left(\frac{v_{\text{EW}}}{f} \right)^2. \end{aligned}$$

This implies that $\lambda_0 \sim \frac{4}{\sqrt{3}} C_t y_t^2$, which could be an order 1 number. Assuming $|\mu_X/\mu_B| = \mathcal{O}(1)$ in Eq. (C5) (and $T_F \gg m_{\text{DM}}$), saturating the relic density would require $m_{\text{DM}} \approx 1$ GeV. This low mass can be achieved by properly tuning the coupling g_B in DM mass expression in Eq. (A19). For $g_R = g_L$, $\lambda_0 = 1$ (leading to $C_t \approx 0.9$) and $C_R = -C_B = 1$, we need to tune $g_B \approx 0.35$ for obtaining $m_{\text{DM}} \approx 1$ GeV, where $f \approx 16$ TeV for avoiding the constraints in Fig. 1 in the main text. As the DM PNGB is nearly massless for this example when $g_B \sim 0.35$, this limit is technically natural according to 't Hooft naturalness principle [57] as it reveals the restoration of a global symmetry.

In the scenario with $\mathcal{R}_R = F$ (fundamental, pseudoreal) of $G_{\text{HC}} = \text{Sp}(2N_{\text{HC}})$, the DM candidate is identified by a complex isosinglet, $\Pi_{CS, \overline{CS}}$, where its mass is given by

$$m_{\Pi_{CS}}^2 = 2(C_B g_B^2 - C_R \tilde{g}_R^2 + C_t y_t^2 s_{\theta_L}^2) f^2, \quad (\text{A22})$$

where $\tilde{g}_R^2 = (3g_R^2 + g_{Y'}^2)/2$, which is always positive. Due to the fact that $s_{\theta_L} \ll 1$, $m_{\Pi_{CS}}^2$ is negative when $C_B g_B^2 = 0$ and therefore a small DM mass, $m_{\Pi_{CS}} \ll f$, can be achieved by tuning $C_B g_B^2$ to a certain value of order unity. Furthermore, in the scenarios with the top mass arising from PC operators, the DM mass can also be tuned by the term $C_B g_B^2$ to small values in both scenarios. These models are inspired by the work in Ref. [45].

APPENDIX B: EXAMPLES OF THEORIES FEATURING THE TECHNI-COMPOSITE HIGGS MECHANISM

In the main body of the article, we studied in detail one specific model based on a gauge symmetry $\text{Sp}(2N)_{\text{HC}}$ and with fermions in two different representations. However, the same mechanism can be found in many other models, with different possibilities for the L and R cosets, as listed in Tables II and III, respectively. Here we list the quantum numbers of the HC fermions needed to obtain the minimal cosets, for the three classes of HC representations: pseudoreal, real and complex.

Finally, in Table IV we provided some examples of gauge-fermion theories generating various combinations for the L and R cosets. In the cases with $\mathcal{R}_L = \mathcal{R}_R$, the global symmetry is extended to a single simple group that contains the L and R subcosets.

TABLE II. Fermion field content and their charges for the minimal L cosets.

	G_{HC}	$\text{SU}(2)_L$	$\text{SU}(2)_R$	$\text{U}(1)_{Y'}$	$\text{U}(1)_{TB,L}$
Pseudoreal					
(U, D)	\mathcal{R}_L	\square	1	0	0
\tilde{U}	\mathcal{R}_L	1	1	-1/2	0
\tilde{D}	\mathcal{R}_L	1	1	+1/2	0
Complex					
(U, D)	\mathcal{R}_L	\square	1	0	1
\tilde{U}	\mathcal{R}_L	1	1	-1/2	1
\tilde{D}	\mathcal{R}_L	1	1	+1/2	1
(U^c, D^c)	\mathcal{R}_L^*	\square	1	0	-1
\tilde{U}^c	\mathcal{R}_L^*	1	1	+1/2	-1
\tilde{D}^c	\mathcal{R}_L^*	1	1	-1/2	-1
Real					
(U, D)	\mathcal{R}_L	\square	1	1/2	0
(\tilde{U}, \tilde{D})	\mathcal{R}_L	\square	1	-1/2	0
X	\mathcal{R}_L	1	1	0	0

TABLE III. Fermion field content and their charges for the minimal R cosets.

	G_{HC}	$\text{SU}(2)_L$	$\text{SU}(2)_R$	$\text{U}(1)_{Y'}$	$\text{U}(1)_X$	$\text{U}(1)_{TB,R}$
Pseudoreal						
(C, S)	\mathcal{R}_R	1	\square	0	+1	0
\tilde{C}	\mathcal{R}_R	1	1	-1/2	-1	0
\tilde{S}	\mathcal{R}_R	1	1	+1/2	-1	0
Complex						
(C, S)	\mathcal{R}_R	1	\square	0	+1	1
\tilde{C}	\mathcal{R}_R^*	1	1	-1/2	-1	-1
\tilde{S}	\mathcal{R}_R^*	1	1	+1/2	-1	-1
Real						
(C, S)	\mathcal{R}_R	1	\square	0	+1	0
\tilde{C}	\mathcal{R}_R	1	1	-1/2	-1	0
\tilde{S}	\mathcal{R}_R	1	1	+1/2	-1	0

TABLE IV. Examples of gauge fermion theories leading to the techni-composite Higgs models.

G_{HC}	\mathcal{R}_L	$\dim(\mathcal{R}_L)$	\mathcal{R}_R	$\dim(\mathcal{R}_R)$	Annotations
$\text{Sp}(2N)_{\text{HC}}$	F	$2N$	$\text{SU}(4)/\text{Sp}(4)_L \otimes \text{SU}(4)/\text{SO}(4)_R \otimes \text{U}(1)_{\Theta}/\emptyset$	$N(2N-1)-1$	N odd to avoid Witten anomalies
$\text{Sp}(2N)_{\text{HC}}$	F	$2N$	Adj	$N(2N+1)$	N even to avoid Witten anomalies
$\text{SU}(4)_{\text{HC}}$	F	4	$\text{SU}(4)^2/\text{SU}(4)_L \otimes \text{SU}(4)/\text{SO}(4)_R \otimes \text{U}(1)_{\Theta}/\emptyset \otimes \text{U}(1)_{\text{TB},L}$	6	...
$\text{SO}(10)_{\text{HC}}$	$Spin$	16	F	10	...
$\text{SU}(5)_{\text{HC}}$	F	5	$\text{SU}(4)^2/\text{SU}(4)_L \otimes \text{SU}(2)^2/\text{SU}(2)_R \otimes \text{U}(1)_{\Theta}/\emptyset \otimes \text{U}(1)_{\text{TB},L} \otimes \text{U}(1)_{\text{TB},R}$	10	...
$\text{SO}(7)_{\text{HC}}$	F	7	$\text{SU}(5)/\text{SO}(5)_L \otimes \text{SU}(4)/\text{SO}(4)_R \otimes \text{U}(1)_{\Theta}/\emptyset$	8	...
$\text{Sp}(2N)_{\text{HC}}$	A	$N(2N-1)-1$	$\text{SU}(5)/\text{SO}(5)_L \otimes \text{SU}(4)/\text{Sp}(4)_R \otimes \text{U}(1)_{\Theta}/\emptyset$	$2N$	$N \geq 2$
$\text{SU}(4)_{\text{HC}}$	A	6	$\text{SU}(5)/\text{SO}(5)_L \otimes \text{SU}(2)^2/\text{SU}(2)_R \otimes \text{U}(1)_{\Theta}/\emptyset \otimes \text{U}(1)_{\text{TB},R}$	4	...
$\text{SO}(10)_{\text{HC}}$	F	10	$Spin$	16	...
$\text{Sp}(2N)_{\text{HC}}$	F	$2N$	$\text{SU}(8)/\text{Sp}(8)$	$2N$...
$\text{SU}(4)_{\text{HC}}$	A	6	$\text{SU}(9)/\text{SO}(9)$	6	...
$\text{SO}(10)_{\text{HC}}$	F	10	F	10	...
$\text{SU}(N)_{\text{HC}}$	F	N	$\text{SU}(6)^2/\text{SU}(6) \otimes \text{U}(1)_{\text{TB}}$	N	...
$\text{SU}(5)_{\text{HC}}$	A	10	F	10	...

APPENDIX C: ASYMMETRY SHARING

We here in detail show how the asymmetric dark matter relic can be calculated [38,50]. First, note that at high temperatures the particle number density n_+ and the antiparticle number density n_- of a given species are given by

$$n_{\pm} = g \int \frac{d^3k}{(2\pi)^3} \frac{g}{e^{(E \mp \mu)\beta} - \eta} \quad \text{with} \quad \begin{cases} \eta = +1 & \text{for bosons} \\ \eta = -1 & \text{for fermions} \end{cases}, \quad (\text{C1})$$

where g is the number of internal degrees of freedom, μ is the chemical potential of the particle species and $\beta = 1/T$ (with $k_B = 1$). At the freeze-out temperature of sphalerons, T_F , we have $\mu/T_F \ll 1$ such that the difference in particle numbers of a given species is given by

$$n = n_+ - n_- = gT_F^3 \frac{\mu}{T_F} \frac{\sigma(m/T_F)}{6}, \quad (\text{C2})$$

which reveals that the chemical potentials are the relevant quantities. Here the statistical suppression factor σ is

$$\sigma(m/T_F) = \begin{cases} \frac{6}{4\pi^2} \int_0^\infty dx x^2 \cosh^{-2} \left(\frac{1}{2} \sqrt{x^2 + (m/T_F)^2} \right) & \text{for fermions} \\ \frac{6}{4\pi^2} \int_0^\infty dx x^2 \sinh^{-2} \left(\frac{1}{2} \sqrt{x^2 + (m/T_F)^2} \right) & \text{for bosons} \end{cases}. \quad (\text{C3})$$

The statistical factor $\sigma(m/T_F)$ is normalized such that

$$\lim_{m/T_F \rightarrow 0} \sigma(m/T_F) = \begin{cases} 1 & \text{for fermions} \\ 2 & \text{for bosons} \end{cases}, \quad (\text{C4})$$

while $\sigma(m/T_F) \simeq 2(m/2\pi T_F)^{3/2} e^{-m/T_F}$ for large $m/T_F \gg 1$. In terms of chemical potentials, the ratio of DM and baryon energy densities can be expressed as

$$\frac{\Omega_{\text{DM}}}{\Omega_B} = \frac{\frac{1}{2} m_{\text{DM}}}{m_P} \left| \frac{\mu_X}{\mu_B} \right| \sigma \left(\frac{m_{\text{DM}}}{2T_F} \right), \quad (\text{C5})$$

where we neglected the $\sigma(m/2T_F)$ for the SM fermions. The task is then to calculate the total chemical potential μ_X of all fermions charged under $\text{U}(1)_X$ and the total chemical potential of all baryons μ_B

To study the chemical potentials we adopt we adopt the notation of Rytov-Sannino [38] and Harvey-Turner [50]. The equilibrium condition from sphalerons, as written

in this convention, was already given in the main text. Additionally, the 6-fermion operators, given by Eq. (A11), lead to equilibrium conditions of the form

$$\begin{aligned}\mu_{UL} - \mu_{UR} + \mu_{SR} - \mu_{SL} - \mu_{uL,i} + \mu_{uR,i} &= 0, \\ \mu_{UL} - \mu_{UR} + \mu_{SR} - \mu_{SL} + \mu_{dL,i} - \mu_{dR,i} &= 0, \\ \mu_{UL} - \mu_{UR} + \mu_{SR} - \mu_{SL} - \mu_{\nu L,i} + \mu_{\nu R,i} &= 0, \\ \mu_{UL} - \mu_{UR} + \mu_{SR} - \mu_{SL} + \mu_{eL,i} - \mu_{eR,i} &= 0,\end{aligned}\quad (\text{C6})$$

and

$$\begin{aligned}\mu_{DL} - \mu_{DR} + \mu_{CR} - \mu_{CL} - \mu_{uR,i} + \mu_{uL,i} &= 0, \\ \mu_{DL} - \mu_{DR} + \mu_{CR} - \mu_{CL} + \mu_{dR,i} - \mu_{dL,i} &= 0, \\ \mu_{DL} - \mu_{DR} + \mu_{CR} - \mu_{CL} - \mu_{\nu R,i} + \mu_{\nu L,i} &= 0, \\ \mu_{DL} - \mu_{DR} + \mu_{CR} - \mu_{CL} + \mu_{eR,i} - \mu_{eL,i} &= 0,\end{aligned}\quad (\text{C7})$$

where the index i refers to the three generations of SM fermions, each of which has equilibrium conditions of this form. However, depending on the temperature, only some generations of quarks and leptons have efficient 6-fermion operators. As was pointed out in the paper, a fermion ψ , receiving its mass m_ψ from such an interaction is in equilibrium at a temperature T if [48,49]

$$2.3 \times 10^4 \times \sqrt{\frac{10 \text{ TeV}}{f}} \frac{m_\psi}{v_{\text{EW}}} \gtrsim \left(\frac{f}{T}\right)^{9/2}. \quad (\text{C8})$$

We assume that the conditions corresponding to (C6) and (C7) apply for any fermions for which the condition (C8) is satisfied for all participating species at the condensation temperature $T = f$.

Furthermore, thermal equilibrium in the electroweak interactions implies the following conditions:

$$\begin{aligned}\mu_{uL,i} &= \mu_{dL,i} + \mu_{WL}, & \mu_{uR,i} &= \mu_{dR,i} + \mu_{WR}, \\ \mu_{eL,i} &= \mu_{\nu L,i} + \mu_{WL}, & \mu_{eR,i} &= \mu_{\nu R,i} + \mu_{WR}, \\ \mu_{DL} &= \mu_{UL} + \mu_{WL}, & \mu_{SL} &= \mu_{CL} + \mu_{WR}.\end{aligned}\quad (\text{C9})$$

The equilibrium is constrained by conditions on the net charge of plasma. To quantify this, consider the eigenvalues of third the components of the isospins of $\text{SU}(2)_{L,R}$, which are

$$\begin{aligned}T_{LL}^3 &= 3 \times \sum_i \left(\frac{1}{2} \mu_{uL,i} - \frac{1}{2} \mu_{dL,i} \right) + \sum_i \left(\frac{1}{2} \mu_{\nu L,i} - \frac{1}{2} \mu_{eL,i} \right) \\ &\quad - 4\mu_{WL} + 2 \left(\frac{1}{2} \mu_{UL} - \frac{1}{2} \mu_{DL} \right),\end{aligned}\quad (\text{C10})$$

$$\begin{aligned}T_{RR}^3 &= 3 \times \sum_i \left(\frac{1}{2} \mu_{uR,i} - \frac{1}{2} \mu_{dR,i} \right) + \sum_i \left(\frac{1}{2} \mu_{\nu R,i} - \frac{1}{2} \mu_{eR,i} \right) \\ &\quad - 4\mu_{WR} + 2 \left(\frac{1}{2} \mu_{CR} - \frac{1}{2} \mu_{SR} \right).\end{aligned}\quad (\text{C11})$$

The overall electric charge, $Q = T_{LL}^3 + T_{RR}^3 + Y'$, is then

$$\begin{aligned}Q &= 3 \times \sum_i \left(\frac{2}{3} \mu_{uL,i} + \frac{2}{3} \mu_{uR,i} - \frac{1}{3} \mu_{dL,i} - \frac{1}{3} \mu_{dR,i} \right) \\ &\quad + \sum_i \left(-1\mu_{eL,i} - 1\mu_{eR,i} + 0\mu_{\nu L,i} + 0\mu_{\nu R,i} \right) \\ &\quad + d(\mathcal{R}_L) \left(\frac{1}{2} \mu_{UL} + \frac{1}{2} \mu_{UR} - \frac{1}{2} \mu_{DL} - \frac{1}{2} \mu_{DR} \right) \\ &\quad + d(\mathcal{R}_R) \left(\frac{1}{2} \mu_{CL} + \frac{1}{2} \mu_{CR} - \frac{1}{2} \mu_{SL} - \frac{1}{2} \mu_{SR} \right) \\ &\quad - 4\mu_{WL} - 4\mu_{WR}.\end{aligned}\quad (\text{C12})$$

The conditions imposed depend on the type of phase transition. Above the transition, where $\text{SU}(2)_{L,R}$ are good symmetries, $T_{LL,RR}^3$ must vanish. If the phase transition is sudden, i.e., first order, then this property is assumed to be inherited by the relic such that the relevant condition is

$$Q = 0, \quad T_{LL}^3 = 0, \quad T_{RR}^3 = 0. \quad (\text{C13})$$

Below the transition, $\text{SU}(2)_{L,R}$ are broken, such that $T_{LL,RR}^3$ need no longer vanish. If the phase transition is gradual, i.e., second order, then this leads to violation of $T_{LL,RR}^3$ conditions. Instead, the VEV drives the chemical potentials of neutral condensates to zero, such that the relevant condition is

$$Q = 0, \quad \mu_{UL} - \mu_{UR} = 0, \quad \mu_{CR} - \mu_{CL} = 0. \quad (\text{C14})$$

We are ultimately interested in comparing the total baryon and DM densities, which depend on the total chemical potentials of the baryons and technibaryons [charged under $\text{U}(1)_X$], which are

$$\mu_B = \sum_i (\mu_{uL,i} + \mu_{uR,i} + \mu_{dL,i} + \mu_{dR,i}), \quad (\text{C15})$$

$$\mu_X = d(\mathcal{R}_R) (\mu_{CR} + \mu_{CL} + \mu_{SL} + \mu_{SR}). \quad (\text{C16})$$

Solving all the above conditions for μ_X and μ_B we find

$$\left| \frac{\mu_X}{\mu_B} \right| = 2 \left(3 + \frac{L}{B} \right), \quad (\text{C17})$$

if 6-fermion operations are inefficient for at least one generation but efficient for at least one other generation. Since the occupation numbers are proportional to the chemical potentials, we can identify $|\mu_X/\mu_B| = |X/B|$. If all generations are in equilibrium, then the lepton number

is constrained to $L = -3B$ so that $\mu_X = 0$. Furthermore, if 6-fermion operators are inefficient for all generations, then μ_X is unconstrained in the case of first-order transitions while Eq. (C17) applies for the case of second-order transitions.

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