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Quantum surface effects in strong coupling dynamics

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Plasmons in nanostructured metals are widely utilized to trigger strong light-matter interactions with quantum light sources. While the nonclassical behavior of such quantum emitters (QEs) is well understood in this context, the role of quantum and surface effects in the plasmonic resonator is usually neglected. Here, we combine the Green's tensor approach with the Feibelman d -parameter formalism to theoretically explore the influence of quantum surface effects in metal-dielectric layered nanostructures on the relaxation dynamics of a proximal two-level QE. Having identified electron spill-out as the dominant source of quantum effects in jellium-like metals, we focus our study on sodium. Our results reveal a clear splitting in the emission spectrum, indicative of having reached the strong coupling regime, and, more importantly, non-Markovian relaxation dynamics of the emitter. Our findings establish that strong light-matter coupling is not suppressed by the emergence of nonclassical surface effects in the optical response of the metal.

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Introduction. Confining light in subdiffraction volumes via surface plasmon polaritons (SPPs) has become common practice to enhance nanoscale light-matter interactions in the past decade [1]. In combination with multilevel quantum emitters (QEs), plasmonic nanostructures play the role of the cavity [2–5] in cavity quantum electrodynamics (QED) [6,7], while the QEs, depending on the desired functionality, can be natural (atoms, molecules) or artificial (quantum wells and dots, defects in nanodiamonds, collective states in transition metal dichalcogenides or hexagonal boron nitride) [8–13]. Advanced fabrication techniques now enable the engineering of metal cavities with characteristic dimensions below 10 nm, as well as precise positioning of QEs within them, to produce promising templates for bright single-photon emitters [14–18]. The plasmonic cavity is typically formed by a metallic substrate interacting with another metallic film or with dropcasted nanoparticles; separating the two plasmonic components by a thin dielectric spacer containing QEs in the form of defects, molecules, or quantum dots [19–22], the resulting intense electromagnetic (EM) fields, confined within minimized volumes, trigger extreme light-matter interactions.

Traditionally, in the local-response approximation (LRA) [23], the optical response of metals is described through the Drude model, or through experimentally measured bulk permittivities. But, as plasmonic cavities become narrower, the

interaction strengths with the therein confined QEs are overestimated by LRA, as compared to experimental results [24–26], calling for amendment of the theoretical models [27–31]; the main missing element is information about quantum effects in the optical response of the metal. As a first extension of LRA, the hydrodynamic Drude model (HDM), which describes the motion of the compressible free-electron gas as a convective fluid, has met with considerable success [32–35], yet effects associated with electron spill-out still require a self-consistent treatment [36–39]. Unfortunately, *ab initio* optical response calculations for plasmonic structures with sizes on the order of 100 nm at room temperature remain beyond computational reach [40].

A more efficient approach is based on the work of Feibelman [41], who bridged EM and *ab initio* calculations through appropriate surface-response functions, the d parameters (d_{\perp} and d_{\parallel}), which need to be calculated only once for a given surface to be implemented in a quantum-informed surface-response formalism (SRF) [31,42–45]. The full QED problem is then described by quantum-corrected mesoscopic boundary conditions at the metal surface [31,42]. Macroscopic QED [46,47] allows one to directly apply the rigorous Green's function approach developed within LRA, now corrected by SRF, without invoking quantum effects in a quasinormal mode formalism [48–50].

The relaxation process of a QE placed in a nanostructured environment has been extensively investigated in the context of the macroscopic QED theory. The photonic environment provides an enhanced density of optical states—often, but not restrictively, in the form of an optical resonance—at a

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specific energy that, when matched with the transition energy of the QE, leads to considerable QE-environment light-matter coupling-strength enhancement. Usually, the interaction is described within a Lorentzian model of the spectral density which, under strong coupling conditions, leads to a Rabi splitting in the emission spectrum and oscillations in the relaxation dynamics of the QE. However, this approach fails to describe possible partially excited state population trapping effects [51–53]. Here, we go beyond the Lorentzian spectral density model approach, taking into account the influence of the exact QE-nanostructure spectral density on the light-matter interaction strength.

To date, focus has been mostly cast on the interaction of QEs with plasmonic nanostructures described by nonlocal dielectric functions within HDM, identifying significant differences in both weak [54,55] and strong coupling regimes [56,57], as compared to LRA. Here, we go one step further to explore, for the first time, the role of quantum-informed plasmonics in the population dynamics of the QE excited state under strong coupling conditions, where the QE and environment coherently exchange energy. We focus on insulator/metal (IM), insulator/metal/insulator (IMI), and metal/insulator/metal (MIM) geometries [33,58], for which the strong coupling regime proves reachable even when quantum corrections in the metal are taken into account.

Theory. The QE is approximated as a two-level system with ground state $|g\rangle$ and excited state $|e\rangle$, transition frequency ω_0 , and dipole moment $\boldsymbol{\mu}$. Initially, the QE is in the excited state, and the EM field is in its vacuum state $|i\rangle = |e\rangle \otimes |0\rangle$, while the final state is $|f\rangle = |g\rangle \otimes \hat{f}_i^{\dagger}(\mathbf{r}, \omega)|0\rangle$, where the QE relaxes to the ground state by emitting a photon or exciting SPPs dressed states supported by the metallic nanostructures [59], and \hat{f}_i^{\dagger} denotes the bosonic creation operator of the dressed state i . The QE relaxation rate Γ is given by $\Gamma(\mathbf{r}, \omega) = \Gamma_0 \tilde{\Gamma}(\mathbf{r}, \omega)$, where $\Gamma_0 = \omega^3 \mu^2 / 3\pi c^3 \hbar \varepsilon_0$ is the vacuum rate and $\tilde{\Gamma}(\mathbf{r}, \omega)$ is the Purcell factor of a QE placed at $\mathbf{r} = (0, 0, z)$ above a metal/dielectric interface; for a transition dipole moment perpendicular to a single insulator/metal interface, the Purcell factor has the form,

$$\tilde{\Gamma}_z(\mathbf{r}, \omega) = \sqrt{\varepsilon_d} - \frac{3c}{2\omega} \operatorname{Re} \left\{ \int_0^{\infty} dk_s \frac{k_s^3 R_{\text{TM}}}{k_{d,z} k_d^2} e^{2ik_{d,z}z} \right\}, \quad (1)$$

where R_{TM} is the generalized transverse magnetic (TM) Fresnel coefficient [60,61]. We note that the metal-dielectric structures considered here are as close to QED cavities as possible, dominated by a single mode, thus allowing the use of a Purcell factor without ambiguity [62].

Our material of choice is sodium (Na), whose work function is lower than that of the common plasmonic metals gold and silver, so as to focus on electron spill-out effects [63,64]. For the single dielectric/metal interface, the TM reflection coefficients take the form (assuming $d_{\parallel} = 0$, valid for Na) [44],

$$R_{\text{TM}} = \frac{\varepsilon_m k_{d,z} - \varepsilon_d k_{m,z} + i(\varepsilon_m - \varepsilon_d)k_s^2 d_{\perp}(\omega)}{\varepsilon_m k_{d,z} + \varepsilon_d k_{m,z} - i(\varepsilon_m - \varepsilon_d)k_s^2 d_{\perp}(\omega)}, \quad (2)$$

where ε_d and ε_m denote the permittivity of the dielectric (d) and metal (m), respectively, $k_0 = \omega/c$ is the free-space wave vector, $k_j = \sqrt{\varepsilon_j} k_0$ (with $j = m, d$) is the wave vector

of each medium, analyzed in in-plane (k_s) and normal ($k_{j,z} = \sqrt{k_j^2 - k_s^2}$) components. For Na, we use a Drude model $\varepsilon(\omega) = 1 - \omega_p^2 / (\omega^2 + i\omega\gamma)$, with ω_p being the plasma frequency and γ the damping rate, taken as $\hbar\omega_p = 5.9$ eV and $\hbar\gamma = 0.1$ eV, while d_{\perp} is given by Lorentzian-fitted data extracted from *ab initio* calculations for jellium [43,44] (see Supplemental Material [65]).

The relaxation of the quantum emitter is described by its emission spectrum [66,67],

$$S(\omega, \mathbf{r}) = \frac{1}{2\pi} \left| \frac{(\mu^2 \omega^2) / (\varepsilon_0 c^2) \hat{\mathbf{n}} \cdot \mathbf{G}(\omega, \mathbf{r}, \mathbf{r}_d)}{\omega_0 - \omega - \int_0^{\infty} d\omega' J(\omega_0, \omega', \mathbf{r}) / (\omega' - \omega)} \right|^2, \quad (3)$$

in the frequency domain, where $\hat{\mathbf{n}}$ is the unit vector in the direction of the dipole moment, and by the time-dependent QE excited state probability amplitude $c_1(t)$, given by the solution of the integro-differential equation [52,68–70],

$$\frac{dc_1(t)}{dt} = i \int_0^t dt' K(t-t') c_1(t'). \quad (4)$$

The kernel of Eq. (4) is given by $K(\tau) = i e^{i\omega_0 \tau} \int_0^{\infty} d\omega J(\omega_0, \omega, \mathbf{r}) e^{-i\omega \tau}$, where $J(\omega_0, \omega, \mathbf{r}) = \tilde{\Gamma}_z(\omega, \mathbf{r}) / [2\pi \tau_0]$ is the spectral density, $\hbar\omega_0$ is the energy difference between the ground and excited QE states, and $\tau_0 = 1/\Gamma_0(\omega_0)$ is its free-space lifetime [52,68–70]. In Eq. (3), \mathbf{r}_d is the position where the signal is detected, and \mathbf{r} is the position of the QE, while ω is the emission frequency of the combined QE-Na system [66,67]. Equation (3) implies that, if the QE-nanostructure coupling strength is high enough, the emission spectrum will feature a doublet of emission peaks, whose energy difference defines the Rabi splitting $\hbar\Omega$. More details about the macroscopic QED model used can be found in the Supplemental Material [65]. Solving Eq. (4), the population dynamics of the QE is calculated under the rotating wave approximation (RWA), which is well justified under the conditions considered here; as we show in [65], results obtained by relaxing the RWA exhibit the same quantitative behavior [52,70].

Results and discussion. To investigate the role of spill-out on the emission properties of QE, we first revisit the simple IM case involving a single SPP resonance. We note here that, in general, there is a competition between relevant contributions from SPPs and a pseudomode stemming from EM modes with higher in-plane momentum [68,71]; effectively, which contribution dominates depends on the QE-metal separation. In Fig. 1(a) we present the Purcell factor as a function of the QE transition energy, for a QE placed 1 nm away from an air-Na IM interface, as evaluated within LRA and SRF. We directly observe that the highest Purcell factor value within SRF has a redshifted peak value that is one order of magnitude smaller than the corresponding LRA result, and the SPP-originated resonance around $\hbar\omega = \hbar\omega_p / \sqrt{2} = 4.125$ eV becomes significantly broader. These alterations are related to additional material losses due to surface-enabled Landau damping [72]. Nevertheless, at lower frequencies, away from the SPP resonance, the SRF Purcell factor is in fact higher than the one predicted by LRA. Similar results have been discussed in Ref. [44], thus validating the Green's tensor formalism employed here. Interestingly, a second spectral feature appears

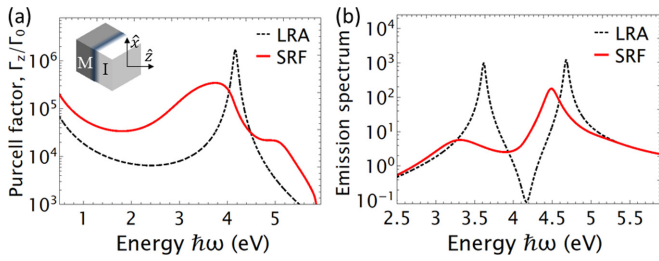


FIG. 1. A QE with z -oriented transition dipole moment, placed 1 nm away from an air/Na IM interface. (a) Purcell factor and (b) emission spectrum (arbitrary units) within LRA (black dashed lines) and SRF (red solid lines).

at around 5 eV as a shoulder in the Purcell spectrum; this is directly related to spill-out, and is known as the Bennett multipole surface plasmon [73,74].

The emission spectrum of a QE with transition energy $\hbar\omega_0 = 4.125$ eV and free-space lifetime $\tau_0 = 0.1$ ns is presented in Fig. 1(b), where the Purcell factors of Fig. 1(a) are used. In the LRA description, the emission spectrum features two sharp peaks, splitting by $\hbar\Omega = 1.06$ eV around the QE transition energy. When the quantum aspects of the response of the metal are introduced through SRF, the two emission peaks become broader, due to the higher material losses, but the Rabi splitting increases to $\hbar\Omega = 1.3$ eV; the latter phenomenon stems from the dependence of the QE emission on the *entire spectrum* of the Purcell factor, which is higher within SRF away from the SPP resonance [Fig. 1(a)] [43].

Turning to the IMI case, where air is considered as the insulating medium, we examine the corresponding Purcell factor in Figs. 2(a) and 2(b) within LRA and SRF, respectively, for metal layer thicknesses $D = 10, 20,$ and 50 nm. Specifically, we set the distance between the QE and the insulator-metal interface to $z_{QE} = 5$ nm, noting that the Purcell factors calculated for the IM and the IMI geometry exhibit negligible differences for smaller values $z_{QE} \sim 2$ nm. In the case of LRA, the Purcell factor has its highest value at the SPP energy for all layer thicknesses. On the other hand, when SRF is taken into account, the maximum Purcell factor is roughly halved, and its peak positions redshift significantly as the metal thickness decreases. For the thinnest layer ($D = 10$ nm), the resonance within SRF has shifted by more than $\hbar\omega = 0.2$ eV compared to LRA. For increasing metal thick-

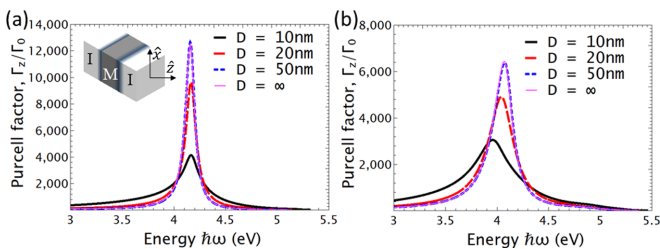


FIG. 2. Purcell factor within (a) LRA and (b) SRF of a QE placed 5 nm away from an IMI nanostructure, for different metal thicknesses $D = 10$ (black solid line), 20 (red dotted line), and 50 nm (blue dashed line). The thin purple curve shows the corresponding IM result.

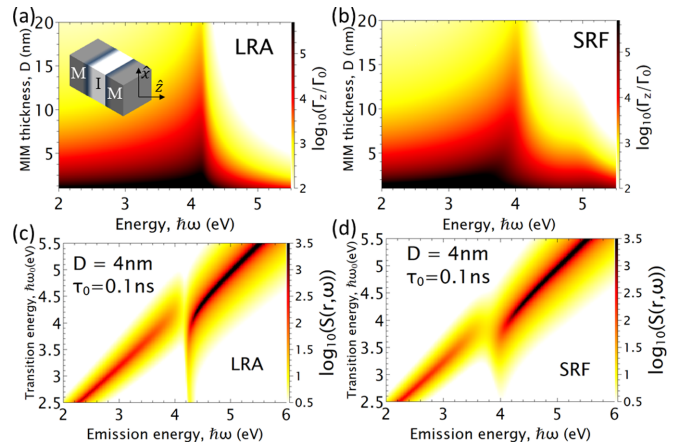


FIG. 3. Contour plot of the Purcell factor of a QE, as a function of emission energy and dielectric layer thickness D , calculated within (a) LRA and (b) SRF, and the corresponding contours of the emission spectra (arbitrary units) as a function of the QE emission and transition energies obtained with (c) LRA and (d) SRF. The QE, with $\tau_0 = 0.1$ ns, is placed in the middle of the insulator layer of an MIM structure with dielectric-layer thickness $D = 4$ nm.

ness (above $D = 50$ nm), the Purcell factor for the IMI case converges to the IM result.

While the IMI architecture can be instructive, in the remainder of the paper we will focus on the MIM structure, which is expected to display many of the advantages of plasmonic cavities discussed in the introduction—apart, perhaps, from the antenna effect that characterizes nanoparticle-on-mirror cavities [5], which contain the QE within them and, when relatively large nanoparticles are involved, one can approximately assume that the QE experiences (locally) the cavity as a MIM. The investigation of QE relaxation inside MIM structures is thus an important first (exactly solvable) step towards understanding timely experimental works.

In Figs. 3(a) and 3(b) we compare LRA and SRF contour plots of the Purcell factor as a function of the QE emission energy and the thickness D of the insulator layer (assumed air here) for a QE placed in the middle of the insulating gap ($z_{QE} = 0$). In both plots, we observe that, for small D , the Purcell factor is significantly enhanced compared to the reference free-space value. In LRA, the peak of the Purcell factor coincides with the SPP resonance, while for higher energies there is a sharp drop of its value, related to the absence of plasmon polariton modes in the bandgap region of the MIM structure [75]. On the other hand, SRF reproduces the expected redshift of the Purcell factor spectrum, while considerable enhancement is observed inside the bandgap, as a result of the quantum effects captured by the Feibelman parameters. As the thickness of the insulator increases, surface effects become less important and the spectra obtained within the two models converge. What is evident from the large Purcell-factor enhancements of Figs. 3(a) and 3(b) is that the QE-MIM interaction can enter the strong coupling regime, as verified by the emission-spectrum contour plots of Figs. 3(c) and 3(d), where clear anticrossings can be observed not only within LRA, but also in the SRF case. Naturally, the emission double-peak features are sharper in the LRA description, and are broadened when additional loss channels due to surface

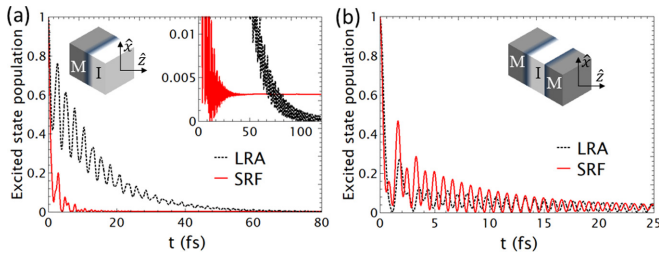


FIG. 4. Population of the excited state of a two-level QE with $\hbar\omega_0 = 3$ eV and $\tau_0 = 0.5$ ns, as a function of time t . (a) The QE is placed 1 nm away from an IM geometry. (b) The QE is placed in the middle of a MIM geometry with dielectric-layer thickness $D = 2$ nm. In both panels, black and red lines correspond to results within LRA and SRF, respectively.

effects are considered, but the observed Rabi splitting clearly survives.

Having established the strong coupling regime, we turn now to the main focus of this paper, which is the QE dynamics. The QE excited-state population dynamics presented in Fig. 4 exhibits strong oscillations, with very different features from simple exponential relaxation within the Markovian (weak coupling) approximation, where memory effects in Eq. (4) are ignored. For a QE with transition energy $\hbar\omega_0 = 3$ eV and vacuum relaxation rate $\tau_0 = 0.5$ ns, Fig. 4(a) shows the excited-state dynamics when $z_{\text{QE}} = 1$ nm in the IM geometry. In the LRA description, we observe that the relaxation follows an exponential pattern modified by rapid oscillations, where after a few of them the QE relaxes to the ground state within a time span of 60 fs. Faster relaxation to the ground state is predicted in SRF, although closer inspection of the inset in Fig. 4(a) reveals that the excited state remains partially populated, $|c_{\text{NL}}|^2 = 0.003$, even at longer times, although it is expected to fully relax due to interaction with the environment.

To directly compare the IM and MIM geometries, we consider a QE centered in an insulating (air) layer of $D = 2$ nm thickness sandwiched between metal regions, i.e., maintaining a 1-nm distance from the metal/dielectric interfaces. Here, the QE population dynamics presented in Fig. 4(b) is characterized by strong oscillatory behavior, with larger population values persisting over longer time spans. While in LRA calculations the QE eventually relaxes to the ground state within the considered time scale, the SRF calculations accounting for the quantum response predict that $\sim 3\%$ of the initial population remains in the excited state on the same time scale, a 10-fold increase compared to the IM structure. The time scale of the plot is short compared to the QE lifetime, and complete relaxation will ultimately be achieved.

In Fig. 5 we present the excited-state population dynamics of a QE placed in the middle of a MIM cavity having an insulator (air) layer thickness of $D = 2$ nm when different free-space relaxation rates τ_0 are considered. Choosing the associated QE transition energy matching the highest value shown in the Purcell factor spectra of Fig. 3, LRA and SRF models are contrasted in Figs. 5(a) and 5(b) for $\hbar\omega_0 = 4.13$ eV and $\hbar\omega_0 = 3.43$ eV, respectively. In both panels we observe strong and rapid Rabi oscillations; as the value of

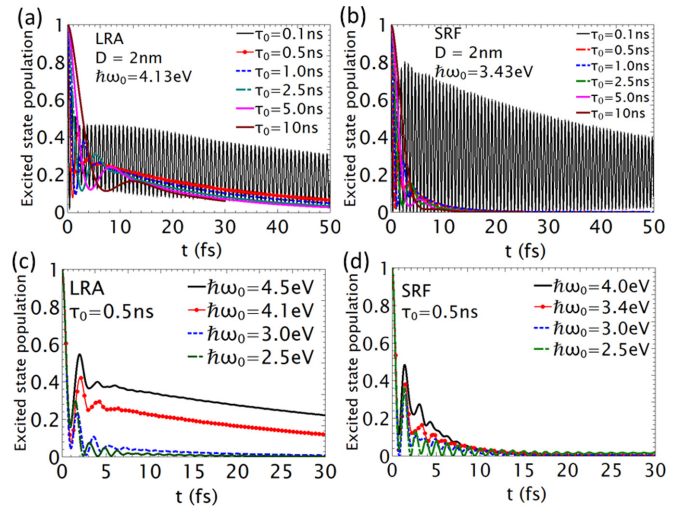


FIG. 5. Population of the excited state of a two-level QE as a function of time, within LRA [(a) and (c)] and SRF [(b) and (d)]. The QE is placed in the middle of a MIM geometry of thickness $D = 2$ nm. (a) and (b) The values of τ_0 considered are displayed in the insets. The transition energy of the QE is $\hbar\omega_0 = 4.13$ eV (LRA) and $\hbar\omega_0 = 3.43$ eV (SRF). (c) and (d) The values of $\hbar\omega_0$ considered are shown in the insets, for a QE with $\tau_0 = 0.5$ ns.

the free-space lifetime decreases from $\tau_0 = 10$ to 0.1 ns, the QE-MIM coupling increases, the oscillation period decreases, and non-Markovian effects become stronger, as anticipated. We also observe that the population oscillations are denser in the SRF case; the reason is that what is considered is the full Purcell-factor spectrum which, compared to the LRA case is broader, and the contribution to the bandgap region is also substantial, thus leading to a higher QE-MIM cavity interaction. The different values of τ are connected with different possible natural or artificial QEs available for experimental realization [13,76,77].

Finally, in Figs. 5(c) and 5(d) we explore the influence of the QE transition energy $\hbar\omega_0$ on the population dynamics, taking a QE free-space lifetime of $\tau_0 = 0.5$ ns. Different values of the QE transition energy are considered, including those matching the SPP energies indicated in the Purcell factor spectrum of Fig. 3. Figure 5(c) shows the LRA calculation, where we observe that, after a few oscillations, the population dynamics remains partially trapped—although, eventually, it fully relaxes at later times. As the QE transition energy decreases, moving away from the SPP resonance energy associated with the highest Purcell factor enhancement, the partially transient trapped population steadily decreases. In the SRF case, we also observe a highly oscillatory behavior of the excited state population density, a sign that the non-Markovian signature is retained. Although the partially excited population trapping is smaller, strong oscillations are still present, with reduced period, indicating that the overall QE-MIM interaction is higher when the quantum aspects of the metal response are taken into account.

Summary. We theoretically explored the emission properties of a QE placed in proximity to IM, IMI, and MIM geometries in the weak and strong coupling regimes. Focusing on Na as a plasmonic metal whose nano-optical response is

dominated by electron spill-out, we adopted the quantum-informed SRF approach, in which the Feibelman d parameters for the centroid of induced charge incorporate first-principles calculations. Although quantum effects introduce additional losses in the metal, the QE-MIM cavity system is found to operate in the strong coupling regime, manifested as a Rabi splitting in the emission spectrum and through Rabi oscillations in the relaxation dynamics of the QE excited state, with a highly non-Markovian character. SRF bridges, therefore, *ab initio* approaches with classical EM calculations in a simple and elegant way, suitable not only for

classical but also for quantum-optical dynamic studies at the nanoscale.

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