The universal Higgs fit

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ABSTRACT: We perform a state-of-the-art global fit to all Higgs data. We synthesise them into a ‘universal’ form, which allows to easily test any desired model. We apply the proposed methodology to extract from data the Higgs branching ratios, production cross sections, couplings and to analyse composite Higgs models, models with extra Higgs doublets, supersymmetry, extra particles in the loops, anomalous top couplings, and invisible Higgs decays into Dark Matter. Best fit regions lie around the Standard Model predictions and are well approximated by our ‘universal’ fit. Latest data exclude the dilaton as an alternative to the Higgs, and disfavour fits with negative Yukawa couplings. We derive for the first time the SM Higgs boson mass from the measured rates, rather than from the peak positions, obtaining $M_h = 124.4 \pm 1.6$ GeV.

KEYWORDS: Higgs Physics, Beyond Standard Model, Standard Model

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1 Introduction

After the discovery of a new particle around 125.5 GeV announced by the ATLAS [1] and CMS [2] LHC collaborations during 2012, all LHC and Tevatron collaborations presented at the Moriond 2013 conference their new results based on the full collected data. These include the most important $\gamma\gamma$, $ZZ^*$ and $WW^*$ channels as well as updates to the fermionic channels. Such results will stay with us for next two years until LHC with full energy starts operating. Therefore it is the right moment to analyse their implications.

We want to know if the new particle is the long-waited Standard Model (SM) Higgs boson [3–6]. On one side, the experimental collaborations are measuring its discrete quantum numbers to check if it is a scalar. On the other side, various theoretical groups [7–36] started to approximatively reconstruct from data its production cross section and its decay modes and consequently its couplings to check if they agree with the SM predictions or with other models beyond the SM. Clearly, this is a more significant test that can be precisely done only by the experimental collaborations, which indeed started to present analyses
along these lines. However these experimental fits, presented in the form of likelihood plots within a few specific beyond-the-SM models, are of little use to theorists who are interested in different models.

We here propose how experimental collaborations could report their results in a model-independent and useful way, such that these results would be readily and reliably used by theorists who want to test any desired model. The new ingredient that we introduce and that allows for this simplification is the assumption that new physics can be approximated as a first-order perturbation with respect to the SM predictions. We find that this assumption is increasingly supported by measurements, that agree with the SM with precisions around the 20% level.

Such results, obtained after two years of LHC operation and with only 25/fb data per experiment, imply severe constraints on models where the Higgs boson is a portal to new physics. We analyse several models and rule out alternative scenarios to the Higgs boson.

The paper is organised as follows. In section 2 we present the data and our fitting procedure. In section 3 we derive the first measurement of the Higgs mass from the rates, rather than from the position of the peaks in the $\gamma\gamma$ and $ZZ$ invariant mass distributions. In section 4 we present the ‘universal’ format for data mentioned above. Next, in section 5 we present fits in various specific models, updating our previous results [37, 38] and comparing the full fit to the simplified ‘universal’ fit to verify that it is a good approximation. We fit Higgs cross sections in section 5.1, Higgs couplings in 5.2, composite Higgs models in 5.3, new physics in loops in 5.4, two Higgs doublet models in 5.5, the MSSM in 5.6, the dilaton in 5.7, the Higgs invisible width in 5.8 and models where DM couples to the Higgs in 5.9. In section 6 we summarise the results and draw our conclusions.

2 The data

Searches for the SM Higgs boson have been carried out in proton-proton collisions at $\sqrt{s} = 7$ (2011 data) and 8 TeV (2012 data) with about 25/fb of total integrated luminosity at the LHC and in proton-antiproton collisions at $\sqrt{s} = 1.96$ TeV at the Tevatron.

There are four main production modes for Higgs boson from $pp$ collisions. The gluon-gluon fusion production mode has the largest cross section, followed in turn by vector boson fusion (VBF), associated $Wh$ and $Zh$ production, and production in association with top quarks, $t\bar{t}h$. The cross sections for the Higgs boson production modes and the decay branching fractions, together with their uncertainties, are taken from [39–44].

Our updated analysis uses the new data presented at the Moriond 2013 conference by the CMS, ATLAS and Tevatron collaborations [45–50] in the following five decay modes: $\gamma\gamma$ [51, 52], $ZZ^*$ (followed by $ZZ^*$ decays to $4\ell$, $2\ell2\nu$, $2\ell2q$, $2\ell2\tau$) [53, 54], $WW^*$ (followed by $WW^*$ decays to $\ell\nu\ell\nu$, $\ell\nuqq$) [46, 47, 55–57], $\tau^+\tau^-$ (followed by leptonic and hadronic decays of the $\tau$-leptons) [58, 59] (we include the CMS $\tau^+\tau^-$ results updated at the end of 2013 [60]) and $b\bar{b}$ [50, 61, 62] (the ATLAS $b\bar{b}$ result was updated at the EPS HEP 2013 [63]), and the first tentative measurements in the $\mu^+\mu^-$ [64], $Z\gamma$ [65, 66] and $WWW$ [67] channels, as well as their combination [68–70]. We also include the $t\bar{t}h$ rate presented by ATLAS at the
Moriond 2014 conference [71]. Here and throughout, $\ell$ stands for electrons or muons and $q$ for quarks.

For a given Higgs boson mass, the search sensitivity depends on the production cross section of the Higgs boson, its decay branching fraction into the chosen final state, the signal selection efficiency, the mass resolution, and the level of standard model backgrounds in the same or a similar final state. For low values of the Higgs boson mass, the $h \rightarrow \gamma\gamma$ and $h \rightarrow ZZ^{*} \rightarrow 4\ell$ channels play a special role due to the excellent mass resolution for the reconstructed diphoton and four-lepton final states, respectively. The $h \rightarrow WW^{*} \rightarrow \ell\nu\ell\nu$ channel provides high sensitivity but has relatively poor mass resolution due to the presence of neutrinos in the final state. The sensitivity in the $bb$ and $\tau^{+}\tau^{-}$ decay modes is reduced due to the large backgrounds and poor mass resolutions.

We include in our data-set all exclusive $\gamma\gamma$ and $\tau\tau$ sub-categories described by the experimental collaborations by telling how much each Higgs production channel in the SM contributes to the various rates. Such information is fully included in our analysis. We adopt the latest $\gamma\gamma$ data MultiVariate Analysis (MVA) from CMS. The two CMS $\gamma\gamma$ analyses (cut-based and MVA) show different signal rates (compatible within 1$\sigma$), and the latter one is closer to the SM. We combine all experiments finding an average $\gamma\gamma$ rate very close to the SM prediction. Consequently our results differ from previous analyses [7–36] performed without including the latest CMS $\gamma\gamma$ data.

This is an important issue because, while most of the presented LHC results are consistent with the SM predictions within experimental errors, there are a few unexpected new developments that warrant additional discussion. The most important of them is the discrepancy between the ATLAS and CMS results in the $h \rightarrow \gamma\gamma$ channels. With full integrated luminosity datasets, ATLAS finds an overall rate of $1.65 \pm 0.34$, higher than the SM prediction of 1, and higher than the CMS result of $0.80 \pm 0.30$. The two measurements are compatible within 2$\sigma$. Finally, the two Higgs boson mass determinations in ATLAS, from the peaks in the $\gamma\gamma$ and $ZZ$ channels, differ by 2$\sigma$. Both experiments have cross checked their analyses and reached conclusions that these deviations appear to be due to statistical fluctuations of both signal and background. This conclusion implies that: (i) combining all data in a global fit is meaningful and increases the precision; (ii) selecting instead any single measurement, for example the ATLAS excess in $\gamma\gamma$, is not justified and would introduce a bias in the data.

The experimental collaborations report Higgs boson rates $R$ in units of the central value of the SM prediction. Their results could be fully encoded in a likelihood $L(R, M_h)$, but only a limited amount of information is reported by the experiments. Often the experimental collaborations report the measured rates as $R^{\exp} \pm R^{\err}$; we use the results in this form whenever available. Sometimes collaborations only report the upper bounds on rates at 95% C.L., $R^{\limit}_{\observed}$, and the expected upper bound at 95% C.L. in absence of a Higgs boson signal, $R^{\limit}_{\expected}$. Assuming that the $\chi^2 = -2 \ln L$ has a Gaussian form in $R$, these two experimental informations allow one to extract the mean $R^{\exp}$ and the standard deviation $R^{\err}$ as $R^{\exp} = R^{\limit}_{\observed} - R^{\limit}_{\expected}$ and $R^{\err} = R^{\limit}_{\expected}/1.96$, where 1.96 arises because 95% confidence level corresponds to about
The measured Higgs boson rates at ATLAS, CMS, CDF, D0 and their average (horizontal gray band at ±1σ). Here 0 (red line) corresponds to no Higgs boson, 1 (green line) to the SM Higgs boson (including the latest data point, which describes the invisible Higgs rate).

2 standard deviations [37].\textsuperscript{1} The χ² is approximated as

\[
\chi^2 = \sum \frac{(R^{\text{exp}}_I - 1)^2}{(R^{\text{err}}_I)^2},
\]

where the sum runs over all measured Higgs boson rates I.

The theoretical uncertainties on the Higgs production cross sections σ\textsubscript{j} start to be non-negligible and affect the observed rates in a correlated way.\textsuperscript{2} We take into account such correlations in the following way. We subtract from the total uncertainty R\textsuperscript{err}\textsubscript{I} the theoretical component due to the uncertainty in the production cross sections, obtaining the purely experimental uncertainty, R\textsuperscript{err−exp}\textsubscript{I}. The theoretical error is reinserted by defining a χ² which depends on the production cross sections σ\textsubscript{j},

\[
\chi^2 = \sum \frac{(R^{\text{exp}}_I - R^{\text{th}}_I(\sigma_j))^2}{(R^{\text{err−exp}}_I)^2} + \sum \frac{(\sigma_j - \sigma_j^{\text{th}})^2}{(\sigma_j^{\text{err}})^2},
\]

and marginalising it with respect to the free parameters σ\textsubscript{j}, constrained to have a central value σ\textsubscript{j}^{\text{th}} and an uncertainty σ\textsubscript{j}^{\text{err}} given e.g. at √s = 8 TeV by [39–44]

\[
\begin{align*}
\sigma(pp \to h)\text{th} &= (19.4 \pm 2.8) \text{ pb}, & \sigma(pp \to jjh)\text{th} &= (1.55 \pm 0.04) \text{ pb}, \\
\sigma(pp \to Wh)\text{th} &= (0.68 \pm 0.03) \text{ pb}, & \sigma(pp \to Zh)\text{th} &= (0.39 \pm 0.02) \text{ pb}, \\
\sigma(pp \to t\bar{t}h)\text{th} &= (0.128 \pm 0.018) \text{ pb}.
\end{align*}
\]

\textsuperscript{1}A similar procedure was described by Azatov et al. in [7].

\textsuperscript{2}Note that the size of the theory uncertainty depends on the applied cuts, and that the scaling of the production cross section to yield the best-fit value relative to the theoretical central value may be different for very different sets of selection cuts (due to the QCD and PDF uncertainties).
See also [72]. We neglect the relatively small uncertainties on the SM theoretical predictions for Higgs branching ratios, dominated by a 4% uncertainty on the $h \to bb$ width.

We summarise all data in figure 1 together with their 1σ error-bars. The grey band shows the ±1σ range for the naive weighted average of all rates: 0.99±0.09. It lies along the SM prediction of 1 (horizontal green line) and is almost 10 σ away from 0 (the horizontal red line is the background-only rate expected in the absence of a Higgs boson).

3 Reconstructing the Higgs mass

The CMS and ATLAS collaborations reported measurements of the pole Higgs mass $M_h$ obtained as the position of the peaks observed in the invariant mass of the $h \to \gamma\gamma$ and $h \to ZZ \to 4\ell$ distributions:

$$M_h = 125.7 \pm 0.4 \text{ GeV} = \begin{cases} 
125.4 \pm 0.5_{\text{stat}} \pm 0.6_{\text{syst}} & \text{GeV CMS } \gamma\gamma \\
125.8 \pm 0.5_{\text{stat}} \pm 0.2_{\text{syst}} & \text{GeV CMS } ZZ \\
126.8 \pm 0.2_{\text{stat}} \pm 0.7_{\text{syst}} & \text{GeV ATLAS } \gamma\gamma \\
124.3 \pm 0.6_{\text{stat}} \pm 0.4_{\text{syst}} & \text{GeV ATLAS } ZZ
\end{cases}. \quad (3.1)$$

These measurements are mutually compatible, and the uncertainty is small enough that in the subsequent fits to rates we can fix $M_h$ to its combined best-fit value. We combined all uncertainties in quadrature, using the standard Gaussian error propagation and neglecting correlations among systematic uncertainties. The averages within each experiment agree with those reported by the experiments. The ATLAS collaboration reports the combined value for the Higgs mass, based on the $\gamma\gamma$ and $ZZ$ channels, as $M_h = 125.5 \pm 0.2_{\text{stat} +0.5_{\text{syst}}}$ (best fit signal strength $R = 1.43 \pm 0.16_{\text{stat}} \pm 0.14_{\text{syst}}$) [73], whereas CMS gives $M_h = 125.7 \pm 0.3_{\text{stat}} \pm 0.3_{\text{syst}}$ based on $\gamma\gamma$, $ZZ$, $WW$, $\tau\tau$ and $bb$ (best fit signal strength $R = 0.80 \pm 0.14$) [74]. Averaging these mass values reproduces the $M_h$ of eq. (3.1).

We here discuss how the Higgs mass can be independently measured, with a larger uncertainty, by requiring that the measured rates agree with their SM predictions within their uncertainties. Such predictions have a dependence on the Higgs mass that, around 125 GeV, can be approximated as

$$\sigma(pp \to X) \approx \sigma(pp \to X)_{M_h=125\text{ GeV}} \times [1 + c_X \times (M_h - 125\text{ GeV})]. \quad (3.2)$$

In table 1 we list the values of the coefficients $c_X$ and of the measured rates for the various processes averaging all experiments, as well as the Higgs mass indirectly derived from such rates. We see that the single best indirect determination of $M_h$ comes from the $h \to WW$ rates, that presently have no sensitivity to $M_h$ if one wants to measure it from a mass peak. We see that best indirect determinations of $M_h$ comes from the $h \to WW$ rates (which presently have no sensitivity to $M_h$ if one wants to measure it from a mass peak) and from $h \to ZZ$. On the other hand, the $h \to \gamma\gamma$ signal that offers the best peak measurement of $M_h$ has very little indirect sensitivity to $M_h$, because the $\gamma\gamma$ rate happens to have a weak dependence on $M_h$. Averaging over all channels we find

$$M_h = 124.4 \pm 1.6 \text{ GeV} \quad \text{(Higgs mass extracted from the rates, assuming the SM)} \quad (3.3)$$
<table>
<thead>
<tr>
<th>Process</th>
<th>$h \rightarrow WW$</th>
<th>$h \rightarrow ZZ$</th>
<th>$h \rightarrow \gamma\gamma$</th>
<th>$Vh \rightarrow Vbb$</th>
<th>$h \rightarrow \tau\tau$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sensitivity $c_X$</td>
<td>6.4%/GeV</td>
<td>7.8%/GeV</td>
<td>-1.5%/GeV</td>
<td>-5.4%/GeV</td>
<td>-4.1%/GeV</td>
</tr>
<tr>
<td>Measured rate/SM</td>
<td>$0.82 \pm 0.16$</td>
<td>$1.08 \pm 0.20$</td>
<td>$1.07 \pm 0.19$</td>
<td>$0.93 \pm 0.36$</td>
<td>$1.17 \pm 0.24$</td>
</tr>
<tr>
<td>Higgs mass in GeV</td>
<td>$122.8 \pm 2.5$</td>
<td>$126.5 \pm 2.5$</td>
<td>$121 \pm 12$</td>
<td>$127 \pm 7$</td>
<td>$121 \pm 6$</td>
</tr>
</tbody>
</table>

Table 1. Determinations of the Higgs mass from the measured Higgs rates, assuming the SM predictions for such rates. We do not use here the independent determination of the Higgs mass from the peak positions in the $\gamma\gamma$ and $ZZ$ energy spectra.

which is compatible with the determination of the pole Higgs mass obtained in a model-independent way from the positions of the peaks.

4 The universal Higgs fit

We perform the most generic fit in terms of a particle $h$ with couplings to pairs of $t, b, \tau, W, Z, g, \gamma$ equal to $r_t, r_b, r_\tau, r_W, r_Z, r_g, r_\gamma$ in units of the SM Higgs coupling. This means, for example, that the coupling to the top is given by $r_t (m_t/V) h\bar{t}t$, where $r_t = 1$ in the SM and $V = 246$ GeV (from the measurement of the Fermi constant [76]) is the Higgs vacuum expectation value. Similarly, the $h\gamma\gamma$ coupling is assumed to be $r_\gamma$ times its SM prediction. In the SM this couplings first arises at one loop level. Experiments are starting to probe also the $h\mu\mu$ and the $hZ\gamma$ effective couplings, so that also the corresponding $r_\mu$ and $r_{Z\gamma}$ parameters will start to be measured. This discussion can be summarised by the following effective Lagrangian:

$$L_h = r_t \frac{m_t}{V} h\bar{t}t + r_b \frac{m_b}{V} h\bar{b}b + r_\tau \frac{m_\tau}{V} h\bar{\tau}\tau + r_\mu \frac{m_\mu}{V} h\bar{\mu}\mu + r_Z \frac{M_Z^2}{V} hZ\bar{Z} + r_W \frac{2M_W^2}{V} hW^+W^- + r_\gamma c_{\gamma\gamma}^{\gamma\gamma} \frac{\alpha}{\pi V} hF_{\mu\nu}F^{\mu\nu} + r_g c_{gSM}^{gg} \frac{\alpha_s}{12\pi V} hG_{\mu\nu}^a G^{a\mu\nu} + r_{Z\gamma} c_{Z\gamma}^{Z\gamma} \frac{\alpha}{\pi V} hF_{\mu\nu}Z_{\mu\nu}. \quad (4.1)$$

The various SM loop coefficients $c_{SM}$ are summarised in appendix A. This Lagrangian is often written in a less intuitive but practically equivalent form by either using SU(2)$_L \otimes$ U(1)$_Y$-invariant effective operators, or assuming that the Higgs is the pseudo-Goldstone boson of a spontaneously broken global symmetry and writing its chiral effective theory [7-36]. We do not consider a modified Higgs coupling to charm quarks, given that $h \rightarrow c\bar{c}$ decays at LHC are hidden by the QCD background. While we cannot exclude that new physics affects $h \rightarrow c\bar{c}$ much more than all other Higgs properties, for simplicity we proceed by discarding this possibility.

Furthermore, we take into account the possibility of Higgs decays into invisible particles $X$, such as Dark Matter or neutrinos [77], with branching ratio $BR_{inv}$. In almost all measured rates (with the exception of the last data-point in figure 1: the direct measurement of the invisible Higgs width) $BR_{inv}$ is equivalent to a common reduction $r$ of all the other Higgs couplings, $BR_{inv} \simeq 1 - r^2$, such that $BR_{inv}$ is indirectly probed by data [37]. The

$^3$The $r_i$ are equivalent to the $\kappa_i$ parametrisation as defined in [75].
Figure 2. $\chi^2$ as function of the model-independent Higgs couplings $r_i$ to the various SM particles, varying them one-by-one (the others are set to unity).

The only observable that directly probes an invisible Higgs width is the $pp \to Zh \to \ell^+\ell^- XX$ rate measured by ATLAS [78, 79] and CMS [80], which implies

$$\text{BR}_{\text{inv}} = -0.18 \pm 0.31. \quad (4.2)$$

Any possible new-physics model can be described as specific values of the $r_i$ parameters. Several examples are provided in section 5.

Following the procedure described in the previous section, we approximatively extract from data the function

$$\chi^2(r_t, r_b, r_\tau, r_W, r_Z, r_g, r_\gamma, r_{Z\gamma}, r_\mu, \text{BR}_{\text{inv}}), \quad (4.3)$$

which describes all the information contained in Higgs data. We find $\chi^2 = 58.3$ at the best fit (58 data points, 10 free parameters), marginally better than the SM fit, $\chi^2_{\text{SM}} = 62.4$ (no free parameters).

4.1 Universal fit to small new physics effects

The universal $\chi^2$ of eq. (4.3) has a too complicated form to be reported analytically, and depends on too many variables to be reported in numerical form, such as plots or tables. For these reasons, previous analyses [7–38] focused on particular BSM models with a reduced number of parameters. For example, figure 2 shows the fit as function of each $r_i$, setting all others to their SM values of unity: we see that the $\chi^2$ are approximately parabolic.

We here observe that Higgs data are converging towards the SM predictions with small errors, thereby it is time to start making the approximation

$$r_i = 1 + \epsilon_i \quad \text{with} \quad \epsilon_i \text{ small} \quad (4.4)$$

and $\text{BR}_{\text{inv}} = \epsilon_{\text{inv}}$. The observable rates $R_I$ are computed at first order in $\epsilon_i$, and consequently the $\chi^2$ is expanded up to second order in $\epsilon_i$. As well known, this Gaussian approximation is a great simplification; for example marginalisations over nuisance parameters just becomes minimisation, which preserves the Gaussian form. Figure 2 suggests
that this approximation already seems reasonably good, particularly in the range of 1 or 2 standard deviations from the central value.

For LHC at 8 TeV the main observables are approximated as

\[
\begin{align*}
R_{h\to WW} &= 1 - 1.14\epsilon_b + 1.58\epsilon_g - \epsilon_{\text{inv}} - 0.04\epsilon_L + 1.72\epsilon_W + 0.02\epsilon_Z - 0.13\epsilon_T \\
R_{h\to ZZ} &= 1 - 1.14\epsilon_b + 1.58\epsilon_g - \epsilon_{\text{inv}} - 0.04\epsilon_L - 0.28\epsilon_W + 2.02\epsilon_Z - 0.13\epsilon_T \\
R_{h\to \tau\tau} &= 1 - 1.14\epsilon_b + 1.58\epsilon_g - \epsilon_{\text{inv}} - 0.04\epsilon_L - 0.28\epsilon_W + 0.02\epsilon_Z + 1.87\epsilon_T \\
R_{h\to \gamma\gamma} &= 1 - 1.14\epsilon_b + 1.58\epsilon_g - \epsilon_{\text{inv}} - 0.04\epsilon_L - 0.45\epsilon_W - 0.06\epsilon_Z - 0.13\epsilon_T + 2\epsilon_{\gamma} \\
R_{h\to bb} &= 1 + 0.86\epsilon_b + 1.58\epsilon_g - \epsilon_{\text{inv}} - 0.04\epsilon_L - 0.28\epsilon_W + 0.02\epsilon_Z - 0.13\epsilon_T \\
R_{V(h\to bb)} &= 1 + 0.86\epsilon_b - 0.17\epsilon_g - \epsilon_{\text{inv}} - 0.05\epsilon_L + 0.83\epsilon_W + 0.67\epsilon_Z - 0.13\epsilon_T,
\end{align*}
\]

(4.5)

where these expressions have been obtained by performing a first-order Taylor expansion in all the \( \epsilon \) parameters of the full non-linear expressions. For all observables but the last one, we have assumed the total Higgs production cross section. When fitting the many real observables, we take into account the relative contribution of each production cross section, as determined by experimental cuts. For \( h \to \gamma\gamma \) we here considered the gluon fusion production channel, and this makes the coefficients of \( \epsilon_{Z,W} \) somehow different from the other channels. The full \( \chi^2 \) can now be reported in a simple form. Indeed the \( \chi^2 \) is a quadratic function of the \( \epsilon_i \), and it is usually written as

\[
\chi^2 = \sum_{ij}(\epsilon_i - \mu_i)(\sigma^2)^{-1}(\epsilon_j - \mu_j), \quad \text{where} \quad (\sigma^2)_{ij} = \sigma_i \rho_{ij} \sigma_j, \quad (4.6)
\]

in terms of the mean values \( \mu_i \) of each parameter \( \epsilon_i \), of its error \( \sigma_i \) and in terms of the correlation matrix \( \rho_{ij} \). We believe that this is the most useful form in which experimental collaborations could report their results. From our approximated analysis of LHC and Tevatron [50] data we obtain:

\[
\begin{align*}
\epsilon_b &= -0.19 \pm 0.30 \\
\epsilon_g &= -0.21 \pm 0.22 \\
\epsilon_{\text{inv}} &= -0.19 \pm 0.25 \\
\epsilon_W &= -0.15 \pm 0.14 \\
\epsilon_Z &= -0.01 \pm 0.13 \\
\epsilon_{\gamma} &= -0.03 \pm 0.16 \\
\epsilon_T &= +0.00 \pm 0.18
\end{align*}
\]

\[
\rho = \begin{pmatrix}
1 & 0.73 & 0.14 & 0.53 & 0.45 & 0.57 & 0.62 \\
0.73 & 1 & 0.51 & 0.44 & 0.27 & 0.44 & 0.59 \\
0.14 & 0.51 & 1 & 0.59 & 0.43 & 0.52 & 0.47 \\
0.53 & 0.44 & 0.59 & 1 & 0.67 & 0.70 & 0.54 \\
0.45 & 0.27 & 0.43 & 0.67 & 1 & 0.61 & 0.49 \\
0.57 & 0.44 & 0.52 & 0.70 & 0.61 & 1 & 0.58 \\
0.62 & 0.59 & 0.47 & 0.54 & 0.49 & 0.58 & 1
\end{pmatrix}
\]

(4.7)

We have not reported the central value of \( r_t = 1 + \epsilon_t \), of \( \epsilon_{Z,\gamma} \) and of \( \epsilon_\mu \) because they presently are known only up to uncertainties much larger than 1. Future searches for t\( b \)h production, for \( h \to Z\gamma \) and for \( h \to \mu^+\mu^- \) will improve the situation.

In many models the Higgs couplings to vectors satisfy \( \epsilon_W = \epsilon_Z \), because of SU(2)_L invariance. Furthermore, in many models LEP precision data force \( \epsilon_W \) and \( \epsilon_Z \) to be very close to 0. This restriction can of course be implemented by just setting these parameters to be equal or vanishing in the quadratic \( \chi^2 \).

Since the uncertainties on the \( \epsilon_i \) parameters are now smaller then 1, the universal approximation starts to be accurate. In the next sections, where we analyze several specific
models, we will systematically compare our full numerical fit (plotting best fit regions in yellow with continuous contours at the 90 and 99% C.L.) with the universal approximation (best fit ellipsoidal regions in gray with dotted contours, at the same confidence levels).

5 Model-dependent Higgs fits

5.1 Higgs production cross sections

Assuming the SM predictions for Higgs decay fractions, we extract from the data the Higgs production cross sections. Given that measured rates of various exclusive and inclusive Higgs channels agree with their SM predictions, we find that production cross sections also agree with SM predictions, as shown in the left panel of figure 3. As expected, the most precisely probed cross section is the dominant one, $\sigma(pp \to h)$. At the opposite extremum $\sigma(pp \to jjh)$ is still largely unknown. The uncertainties on the reconstructed cross sections are correlated, although we do not report the correlation matrix.

5.2 Higgs couplings

We here extract from data the Higgs boson couplings to vectors and fermions, assuming that only the SM particles contribute to the $h \to gg, \gamma\gamma, \gamma Z$ loops. This amounts to restricting the universal fit in terms of the $r_i$ parameters by setting the parameters for loop couplings to

$$r_g = r_t, \quad r_\gamma \approx 1.282 r_W - 0.282 r_t, \quad r_{Z\gamma} \approx 1.057 r_W - 0.057 r_t.$$  (5.1)
These numerical expressions are obtained by rescaling the expressions for the SM loops summarised in appendix A. In particular, the $W$ loop (rescaled by $r_W$) and the top loop (rescaled by $r_t$) contribute to $h \to \gamma\gamma$ with a negative interference.

Under this assumption the top coupling of the Higgs, $r_t$, becomes indirectly probed via the loop effects. The fit to the couplings is shown in figure 3b and agrees with the SM predictions (diagonal line), signalling that the new boson really is the Higgs. The correlation matrix can be immediately obtained by inserting eq. (5.1) into the universal $\chi^2$ of eq. (4.6).

We allow the SM prediction to vary in position and slope by assuming that the Higgs couplings to particles with mass $m$ are given by $(m/v')^p$. Taking into account all correlations, we find that data imply parameters $p$ and $v'$ close to the SM prediction of $m/v$ (diagonal line in the right panel of figure 3):

$$p = 0.99 \pm 0.03, \quad v' = v(0.99 \pm 0.06)$$

with a 27% correlation.

### 5.3 Composite Higgs models

Models where the Higgs is composite often assume the further restriction, in addition to eq. (5.1), of a common rescaling with respect to their SM values of the Higgs boson couplings to the $W, Z$ bosons and a common rescaling of the Higgs boson couplings to all fermions. These rescalings are usually denoted as $a$ and $c$, respectively:

$$r_t = r_b = r_\tau = r_\mu = c, \quad r_W = r_Z = a.$$  

The resulting fit is shown in the left panel of figure 4. We see that our approximated universal fit (dotted contours) reproduces very well our full fit (continuous contours).
best fit converged towards the SM; in particular data now disfavour the solution with \( c < 0 \) which appeared in previous fits. Similar fits by the ATLAS and CMS collaborations are given in [81, 82]. The CMS result is similar to ours, while ATLAS has \( c/a = 0.85^{+0.23}_{-0.13} \), due to their larger \( h \to VV \) rates, which is compatible with our result at 1\( \sigma \) level.

The reason is visualised in the middle panel of figure 4, where we show the bands favoured by the overall rates for Higgs decay into heavy vectors \((WW \text{ and } ZZ)\), that get affected in the same way within the model assumptions), into fermions \((bb \text{ and } \tau\tau)\), that get affected in the same way within the model assumptions) and into \( \gamma\gamma \). We see that these bands only cross around the SM point, \( a = c = 1 \). The full fit to all exclusive rates contains more information than this simplified fit.

In the right panel of figure 4 we show the full \( \chi^2 \) restricted along the trajectories in the \((a, c)\) plane (plotted in the left panel) predicted by simple composite pseudo-Goldstone Higgs models in terms of the parameter \( \xi = (V/F_\pi)^2 \), where \( F_\pi \) is the scale of global symmetry breaking [83, 84], \( F_\pi \approx 130.4 \text{ MeV} \).

### 5.4 New physics only in the loop processes

We assume here that only the loop processes are modified with respect to the SM predictions, summarized in appendix A. This amounts to restricting our universal fit settings

\[
\begin{align*}
    r_t &= r_b = r_\tau = r_\mu = r_W = r_Z = 1, \\
    \frac{\Gamma(h \leftrightarrow gg)}{\Gamma(h \leftrightarrow gg)_{SM}} &= r_g^2, \\
    \frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}} &= r_\gamma^2
\end{align*}
\]

with \( \text{BR}_{inv} = 0 \) and \( r_{Z\gamma} = 1 \). The latter assumption is at present justified because of the large experimental error in the \( h \to Z\gamma \) rate, even though in general new physics in the loop
processes would induce deviation from unity in both \( r_{Z\gamma} \) and \( r_\gamma \). The result is shown in the left panel of figure 5, in the form of a fit to the ratios of \( \text{BR}(h \rightarrow gg) \) and \( \text{BR}(h \rightarrow \gamma\gamma) \) with respect to the SM. One can see that the SM is well within the 1\( \sigma \) contour. The analogous ATLAS result [81, 82] is instead barely compatible with the SM at 2\( \sigma \) level because they only fit ATLAS data, where \( h \rightarrow VV \) rates have a central value above the SM. The universal fit approximates the full fit reasonably well. The dashed trajectories show the loop effect due to extra scalar particles with the same quantum numbers of the top (red), of the bottom (blue), of the tau (vertical black line). The explicit expressions for the contribution of scalar, fermion and vector particles running in the loop can be found in appendix A. Note that any additional colorless but electrically charged particle would lead to the same trajectory obtained for the scalar partner of the \( \tau \).

To better investigate the constraints on a possible new scalar \( S \), in the right panel of figure 5 we show the upper bound, as function of the scalar mass \( m_S \), on the scalar coupling \( r_S \) to the Higgs boson, defined by the coupling

\[
    r_S \frac{2m^2}{V} hSS.
\]

The resulting loop effects are summarised in appendix A. The solid and dashed curves in the right panel of figure 5 are respectively the upper bounds at 90\% (solid) and 99\% (dashed) C.L. More stringent limits are obtained on the top and bottom partners than on the \( \tau \) partner.

One can also use the universal fit with the assumption of eq. (5.4) to derive indirect constraints on the top quark magnetic \( (g_t) \) and chromomagnetic \( (k_t) \) dipole moments [85, 86], which in the SM are expected to be respectively \( g_t \approx 2 \) and \( k_t \approx 2 \). Allowing \( g_t \) and \( k_t \)
Figure 7. Fit to the $t$-quark and to $b$-quark and $\tau$-lepton Yukawa couplings assuming the structure predicted by the various types of two Higgs doublet models. Dotted lines show the Gaussian approximation. The point (1, 1) marked as ‘SM’ is the Standard Model; the point (0, 0) marked as ‘FP’ is the fermiophobic case.

to vary freely, the $h \rightarrow \gamma\gamma$ and $h \rightarrow gg$ amplitudes are modified with respect to the SM as:

$$r_\gamma = \frac{c^{(W)}_\gamma + c^{(t)}_\gamma (3g^2 - \frac{1}{2})}{c^{(W)}_\gamma + c^{(t)}_\gamma}, \quad r_g = \frac{3}{8}k^2 - \frac{1}{2},$$

(5.6)
where the quantities \(c_{W}^{(r)}\) and \(c_{t}^{(r)}\) are defined in eq. (A.4) of the appendix. Numerically we have \(c_{W}^{(r)} = -1.043\) and \(c_{t}^{(r)} = 0.223\). Figure 6 shows the 90% and 99% C.L. allowed regions for \(g_{t}\) and \(k_{t}\). The uncertainty on \(k_{t}\) is comparable to the one from its direct measurements at the LHC and the Tevatron as combined in [87], while the one for \(g_{t}\) is even smaller. The conversion from the results of [87] is done in [85] for \(g_{t}\), giving \(-3.49 < g_{t} < 3.59\), and in [86] for \(k_{t}\), giving \(|k_{t} - 2| < 0.2\) at 95% C.L.

Eq. (5.6) was computed by [85, 86] at the weak scale, in the phase with broken electroweak symmetry. An analogous computation was performed in [88–90], promoting the dipoles to full \(SU(2)_{L} \otimes U(1)_{Y}\)-invariant effective operators with a non-renormalizable dimension \(d > 4\), suppressed by a factor \(1/\Lambda^{d-4}\), \(\Lambda\) being the cutoff of the theory. The result [88–90] is that the dipole operators before electroweak symmetry breaking contribute, via RGE mixing, to other one-loop suppressed operators affecting the \(h \rightarrow \gamma \gamma\) and \(h \rightarrow gg\) decay rates [91]. Finite parts are not computed. Because of the RGE running from \(\Lambda\) down to \(m_{h}\), the effect is proportional to \(\ln \Lambda / m_{h}\), differently from eq. (5.6). Using the operator mixing result of [88–90] and parametrizing the \(d = 6\) dipole operators at \(\Lambda\) via quantities analogous to \(g_{t}\) and \(k_{t}\) but defined at \(\Lambda\), the decay rates [91] can be written as

\[
r_{\gamma} = 1 - \frac{4/3}{c_{W}^{(r)} + c_{t}^{(r)}} \left( \frac{g_{t}(\Lambda)}{2} - 1 \right) \log \frac{\Lambda}{m_{h}}, \quad r_{g} = 1 - \frac{6}{c_{g}^{(r)}} \left( \frac{k_{t}(\Lambda)}{2} - 1 \right) \log \frac{\Lambda}{m_{h}},
\]

where the quantity \(c_{g}^{(r)}\) is defined in eq. (A.4) of the appendix. Numerically \(c_{g}^{(r)} = 1.03\).

Repeating our fit, we obtain similar constraints as illustrated in the right panel of figure 6, for representative values of the cutoff.

5.5 Models with two Higgs doublets

There are four types of two Higgs doublets models (2HDM) where tree-level flavour-changing neutral currents (FCNCs) are forbidden by a \(Z_{2}\) symmetry [92] and both doublets \(H_{1}\) and \(H_{2}\) get a vacuum expectation value:

- type I [93, 94] where only one doublet couples to all quarks and leptons;
- type II [94, 95], where up-type quarks couple to \(H_{2}\) and \(H_{1}\) couples to down-type quarks and leptons. The Higgs sector of the MSSM is a type II 2HDM;
- type X (lepton-specific or leptophilic) where \(H_{2}\) couples only to quarks and \(H_{1}\) couples only to leptons;
- type Y (flipped) [96–101], where \(H_{2}\) couples to up-type quarks and \(H_{2}\) to down-type quarks, and (contrary to the type II HDM) leptons couple to \(H_{2}\).

For an extensive review see [102] and for some previous fits see [103, 104]. The modification to Yukawa couplings to up-type and down-type quarks and leptons in the four 2HDMs is given in table 2. As usual, \(\tan \beta = v_{2}/v_{1}\) is the ratio of the VEVs of the two doublets and \(\alpha\) is the mixing angle of the CP-even mass eigenstates. The SM limit corresponds to \(\beta - \alpha = \pi/2\). In all of the models the vector couplings are also modified as

\[
r_{W} = r_{Z} = \sin(\beta - \alpha).
\]

(5.8)
Table 2. Modification to Yukawa couplings to up-type and down-type quarks and leptons in the four 2HDMs.

<table>
<thead>
<tr>
<th></th>
<th>Type I</th>
<th>Type II</th>
<th>Type X (lepton-specific)</th>
<th>Type Y (flipped)</th>
</tr>
</thead>
<tbody>
<tr>
<td>$r_t$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$\cos \alpha / \sin \beta$</td>
</tr>
<tr>
<td>$r_b$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$- \sin \alpha / \cos \beta$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$- \sin \alpha / \cos \beta$</td>
</tr>
<tr>
<td>$r_\tau$</td>
<td>$\cos \alpha / \sin \beta$</td>
<td>$- \sin \alpha / \cos \beta$</td>
<td>$- \sin \alpha / \cos \beta$</td>
<td>$\cos \alpha / \sin \beta$</td>
</tr>
</tbody>
</table>

The results of our fits are presented in figure 7 in terms of the fermion couplings $r_t, r_b, r_\tau$, restricted by the 2HDM models to lie within the green regions. (We do not show the region for $r_{b,\tau} \approx 1$ which is allowed since the measurements have no sensitivity to the signs of these couplings.) We find that in each case, it is $r_t$ that dominates the fit and the bottom contributions to gluon fusion and $h \rightarrow \gamma\gamma$ are negligible. The effect of the charged Higgs boson in the $h \rightarrow \gamma\gamma$ loop is neglected.

The type II 2HDM (upper panel) allows for independent modification of the $t$ coupling $r_t$, and for a common modification of the $b$ and $\tau$ couplings, $r_b = r_\tau$. The former is predicted to be reduced and the latter enhanced by the model. The modification of eq. (5.8) of the vector couplings can be equivalently written as $r_W = r_Z = (1 + r_tr_b)/(r_t + r_b) \approx 1 + \epsilon_t \epsilon_b/2$, showing that it is a small second order effect. In this model a negative $t$ Yukawa coupling is still allowed at slightly more than 99% CL. The red line in the same panel shows the parameter space allowed by type I 2HDM, where all the couplings scale uniformly.

In the flipped 2HDM (middle panel) the $\tau$ Yukawa coupling changes in the same way as the $t$ coupling and the region with negative coupling is disfavoured by data. Finally, in the leptophilic 2HDM (lower panel) the $t$ and $b$ couplings vary in the same way, while the $\tau$ coupling is independent.

The universal fit provides a reasonable approximation to the full fit in all 2HDM models.

### 5.6 Supersymmetry

Supersymmetry can affect Higgs physics in many different ways, such that it is difficult to make general statements. We here focus on the two most plausible effects:

- The stop squark loop affect the $h \leftrightarrow gg, \gamma\gamma, Z\gamma$ rates. Given that the stop has the same gauge quantum numbers of the top, such effects are correlated and equivalent to a modification of the Higgs coupling to the top (as long as it is not directly measured via the $t\bar{t}h$ production cross section) by an amount given by

$$R_t = 1 + \frac{m_t^2}{4} \left[ \frac{1}{m_{t_1}^2} + \frac{1}{m_{t_2}^2} - \frac{(A_t - \mu/\tan \beta)^2}{m_{t_1}^2 m_{t_2}^2} \right]$$

(5.9)

in the limit of heavy stop masses, $m_{t_1,2} \gg m_t$. Notice that $R_t$ can be enhanced or reduced with respect to one, depending on the latter mixing term.

- The type II 2HDM structure of supersymmetric models modifies at tree-level the Higgs couplings, as already discussed in section 5.5.
Figure 8. Left: fit to the two main effects present in supersymmetry: stop loop correction to the $ht\bar{t}$ coupling and tree-level modification of the Higgs couplings due to the two-Higgs doublet structure. Dotted lines show the Gaussian approximation. Right: fit as function of the $\beta$-function coefficients $b_3 = b_\gamma$ that parameterise dilaton models. The SM Higgs is reproduced at the experimentally favored point $b_3 = b_\gamma = 0$, while the pure dilaton is excluded at more than 5$\sigma$.

All of this amounts to specialise the universal $\chi^2$ inserting the following values of its parameters

$$r_t = R_t \frac{\cos \alpha}{\sin \beta}, \quad r_b = r_\tau = r_\mu = -\frac{\sin \alpha}{\cos \beta}, \quad r_W = r_Z = \sin(\beta - \alpha). \quad (5.10)$$

Furthermore, the parameters $r_g, r_\gamma, r_Zr_\gamma$ relative to loop processes are fixed as in eq. (5.1). We trade the $\alpha$ parameter (mass mixing between Higgses) for the pseudo-scalar Higgs mass $m_A$ using

$$\tan 2\alpha = \frac{m_A^2 + M_Z^2}{m_A^2 - M_Z^2} \tan 2\beta. \quad (5.11)$$

Finally, we assume a large tan $\beta$, as motivated by the observed value of the Higgs mass (a large tan $\beta$ amplifies the stop contribution to the Higgs mass). The left panel of figure 8 shows the resulting fit. Once again, the universal fit is an adequate approximation of the full fit. Of course, supersymmetry can manifest in extra ways not considered here, e.g. very light staus or charginos could enhance $h \to \gamma\gamma$ [105–111].

5.7 Data prefer the Higgs to the dilaton

As another example of a model where both the tree-level and the loop level Higgs couplings are modified, we consider the dilaton. The dilaton is an hypothetical particle $\varphi$, that, like the Higgs, couples to SM particles with strength proportional to their masses [112–115]. More precisely the dilaton has a coupling to the trace of the energy-momentum tensor $T_{\mu\nu}$,
suppressed by some unknown scale $\Lambda$:

$$
\frac{\varphi}{\Lambda} T^\mu_\mu = \frac{\varphi}{\Lambda} \left( \sum_f m_f \bar{f} f - M_W^2 Z^\mu_\mu - 2 M_Z^2 W^\mu_\mu + b_3 \frac{\alpha_3}{8\pi} G_a^a G_a^a + b_\gamma \frac{\alpha_{em}}{8\pi} F^\mu_\mu F^\mu_\mu \right). 
$$

(5.12)

The dilaton couplings to $gg$ and $\gamma\gamma$ differ from the corresponding Higgs boson couplings, because eq. (5.12) contains the latter two quantum terms, that are present in $T^\mu_\mu$ because scale invariance is anomalous and broken at quantum level by the running of the couplings. Indeed $b_3$ and $b_\gamma$ are the $\beta$-function coefficients of the strong and electromagnetic gauge couplings. In the SM they have the explicit values $b_3 = -7$ and $b_\gamma = 11/3$: we call ‘pure dilaton’ this special model, which gives a significant enhancement of $h \leftrightarrow gg$.

Models where a dilaton arises usually contain also new light particles, such that $b_3$ and $b_\gamma$ can differ from their SM values. Thereby we perform a generic fit where $b_3$ and $b_\gamma$ are free parameters in addition to $\Lambda$. Then, our universal fit is adapted to the case of the generic dilaton by setting

$$
r \equiv r_W = r_Z = r_t = r_b = r_\tau = \frac{V}{\Lambda}, \quad r_g \approx r(1 - 1.45 b_3), \quad r_\gamma \approx r(1 + 0.15 b_\gamma) \quad (5.13)
$$

where $V = 246$ GeV.

In our previous analyses [37, 38], the dilaton gave fits of comparable quality to the SM Higgs, despite the significantly different predictions of the dilaton: enhanced $\gamma\gamma$ rates and reduced vector boson fusion rates. The first feature is no longer favoured by data, and the second feature is now disfavoured: so we find that present data prefer the Higgs to the ‘pure dilaton’ at about $5\sigma$ level. We then consider the generic dilaton, showing in the right panel of figure 8 that the allowed part of its parameters space is the one where it mimics the Higgs, possibly up to a sign difference in $r_g$ and/or $r_\gamma$. The linear couplings of the dilaton in eq. (5.12) become identical to those of the SM Higgs in the limit $b_3 = b_\gamma = 0$ and $\Lambda = V$. This situation is not easily realisable in models, given that adding extra charged particles increases $b_\gamma$ rather than reducing it; one needs to subtract particles by e.g. assuming that that 3rd generation particles are composite [119].

The universal approximation works reasonably well, although it cannot reproduce these disjoint solutions.

### 5.8 Higgs boson invisible width

Next, we allow for a Higgs boson invisible width, for example into Dark Matter (this does not comprise undetectable decays into known physics, such as Higgs to light jets).\footnote{Note that such decays are only undetectable at hadron colliders due to large QCD backgrounds and trigger problems, but could be detected at an $e^+e^-$ collider in the $ZH$ production mode.} We perform two fits.

1. In the first fit, the invisible Higgs width is the only new physics. We find (blue curves in the left panel of figure 9) that present data imply $\text{BR}_{\text{inv}} = -0.07 \pm 0.15$. The one-sided upper bound, computed restricting to $0 \leq \text{BR}_{\text{inv}} \leq 1$, is

$$
\text{BR}_{\text{inv}} < 0.22 \text{ at } 95\% \text{ C.L.} \quad (5.14)
$$
In addition to the invisible width we also allow for non-standard values of $h \rightarrow \gamma \gamma$ and $h \leftrightarrow gg$, finding a weaker constraint on BR$_{\text{inv}}$ (red curves in figure 9a)

$$\text{BR}_{\text{inv}} < 0.34 \text{ at 95\% C.L.}$$

(5.15)

The reason is that an enhanced $gg \rightarrow h$ production rate can partially compensate for an invisible Higgs width, but a full compensation would be possible only by enhancing all production rates by the same amount. The Higgs coupling to vectors is independently measured to agree with SM predictions from electroweak precision data.

Notice that the main constraint for BR$_{\text{inv}}$ does not come from the direct search for $pp \rightarrow Zh \rightarrow \ell\ell E_T$ (included in our data-set) but from the global fit [37, 116, 117].

5.9 Dark Matter models

The invisible Higgs boson decay width [116, 117] constrains Dark Matter (DM) candidates with mass below $M_h/2$. The Higgs sector of the SM allows for a direct coupling to particles of a hidden sector. If the latter are stable and interact weakly with the SM sector, they could represent viable Dark Matter (DM) candidates. If DM particles have mass below $M_h/2$, the Higgs boson can thus decay into a pair of DM particles, which would escape detection. Invisible Higgs decays are constrained by the fact that the ATLAS and CMS Higgs rates are compatible with the predictions of the SM Higgs boson. The experimental bound on BR$_{\text{inv}}$ can be used to constrain the DM mass and its elastic cross section on
nucleons probed in direct detection experiments, as illustrated for instance in [118], where DM is assumed to be either a scalar $S$, or a Majorana fermion $f$ or a vector $V$ coupled to the Higgs as

$$r_S \frac{2m_S^2}{V} hSS + r_f \frac{m_f}{V} h\bar{f}f + r_V \frac{2m_V^2}{V} hV\mu V_{\mu}.$$ \hfill (5.16)

The partial Higgs decay width into dark matter $\Gamma(h \to DM DM)$ and the spin-independent DM-proton elastic cross section $\sigma_{SI}$ can be calculated in terms of the parameters of the above Lagrangian. Both are proportional to the square of the DM-Higgs coupling, so that the ratio $\mu \equiv \sigma_{SI}/\Gamma(h \to DM DM)$ depends only on the unknown DM mass and on the known masses and couplings of the relevant SM particles (see for instance the expressions provided in [118]).

This allows us to relate the invisible Higgs branching fraction to the DM direct detection cross section:

$$BR_{inv} \equiv \frac{\Gamma(h \to DM DM)}{\Gamma_h^{SM} + \Gamma(h \to DM DM)} = \frac{\sigma_{SI}}{\mu\Gamma_h^{SM} + \sigma_{SI}}$$ \hfill (5.17)

where $\Gamma_h^{SM} = 4.1$ MeV is the total Higgs decay width into all SM particles, that we fix to its SM prediction. For a given DM mass, an upper bound on the Higgs invisible branching fraction implies an upper bound on the DM scattering cross section on nucleons. The relation between the invisible branching fraction and the direct detection cross section strongly depends on the spinorial nature of the DM particle, in particular, the strongest (weakest) bound is derived in the vectorial (scalar) case.

Imposing the upper bounds on $BR_{inv}$ derived in section 5.8, figure 9 shows the corresponding upper limits on the spin-independent DM cross section on nucleons as a function of the DM mass, in the case of scalar (green), Majorana fermion (red) and vector (blue) DM candidates.

In all cases, the derived bounds are stronger than the direct one from LUX2013 as long as the mass of DM is lighter than $M_h/2$. This conclusion does not rely on the assumption that DM is a thermal relic that reproduces the observed cosmological DM abundance. The limit on $\sigma_{SI}$ crucially depends on the assumption that DM directly couples to the Higgs. Larger values of $\sigma_{SI}$ remain possible in different models, where DM couples to the $Z$ or directly to nucleons via loops of supersymmetric or other particles.

6 Discussion and conclusions

The LHC experiments reported their measurements of Higgs boson properties at the Moriond 2013 conferences, based on the full collected luminosity during 2011 and 2012. At the same time, Tevatron reported their final Higgs results. With the crucial inclusion of the full CMS $\gamma\gamma$ data (missing in previous analyses), at this stage all main Higgs results from Tevatron and from the first phase of LHC have been basically presented. Those results will drive our understanding of particle physics, until new 13 TeV LHC data will be available.

Motivated by these results, we have performed a state-of-the-art global fit to Higgs boson data, including all sub-categories studied by the experimental collaborations, for a
total of 56 experimental inputs, as summarised in figure 1. We found that the average Higgs rate is $0.99 \pm 0.09$ in SM units, supporting the SM Higgs boson hypothesis. The Higgs boson mass is usually determined from the peaks in the invariant mass distribution of $ZZ$ and $\gamma\gamma$. We performed the first measurement of the Higgs boson mass from the rates, finding that the two determinations are compatible:

$$M_h = \begin{cases} 125.7 \pm 0.4 \text{ GeV from the peaks,} \\ 124.4 \pm 1.6 \text{ GeV from the rates.} \end{cases}$$ (6.1)

The LHC physics program has been successful: with only $\approx 25/fb$ of data per experiment the Higgs boson has been discovered and several of its properties determined within $\approx \pm 20\%$ precision. We are now entering into the era of precision Higgs physics — deviations from the SM due to new physics no longer can dominate the data. This observation allowed us to propose a ‘universal’ form in which experiments could report their results allowing theorists to easily test any desired model. The new assumption that makes possible this significant simplification is that new physics is a small correction to the SM. While we used all publicly available data to present our own global combination in ‘universal’ form in eq. (4.7), we stress that only the experimental collaborations can perform a fully precise analysis, for example including the correlations among experimental uncertainties.

We studied several new physics scenarios beyond the SM. We determined from data the production cross sections (assuming standard Higgs decays) and the Higgs decays widths (assuming standard productions), finding that they lie along the SM predictions. In a more general context, we allowed all possible Higgs boson couplings to any SM particle to deviate from its SM value, finding that couplings to the $W, Z, t, b, \tau$ must lie around their SM predictions up to uncertainties of about $\pm 20\%$ (see the right panel of figure 3). In particular, non-standard Higgs boson couplings to vectors, predicted by composite Higgs models, are most stringently constrained. The scenario of negative Higgs coupling to fermions (‘dysfermiophilia’) that gave the best fit with early LHC data is now disfavoured at more than $2\sigma$.

We considered various specific new physics models: new scalars, 2HDM, supersymmetry, dilaton, composite Higgs, invisible Higgs decays, possibly into Dark Matter particles, anomalous couplings of the top, etc. The results of those fits are presented in numerous figures throughout the paper. Qualitatively, all reach the same conclusions:

i) best fit regions lie along SM predictions, imposing constraints on new physics;

ii) our simple universal fit is a reasonable approximation to the full fit.

In particular we find that, with the latest data, the dilaton alternative to the Higgs is now excluded at $5\sigma$, with the exception of the special non-minimal dilaton tuned to exactly reproduce the Higgs (section 5.7).

We will update this paper when future results become available.
Acknowledgments

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A New physics contributions to loop processes

The coefficients in the second line of eq. (4.1) arise at one-loop. They are obtained by summing the contributions of all scalars \((S)\) fermions \((f)\) and vectors \((V)\) that couple to the Higgs as in eq. (5.16). The explicit expressions for the loop effects are \([121]\):

\[
\begin{align*}
    c_\gamma^{(S)} &= \frac{C_\gamma^S}{2} r_{\gamma S} A_{\gamma S}(\tau_S) &
    c_\gamma^{(f)} &= 2 C_\gamma^f r_f A_f(\tau_f) \\
    c_\gamma^{(S)} &= \frac{N_S Q_S^2}{24} r_{\gamma S} A_{\gamma S}(\tau_S) &
    c_\gamma^{(f)} &= \frac{N_f Q_f^2}{6} r_f A_f(\tau_f) &
    c_\gamma^{(V)} &= -\frac{7 Q_V^2}{8} r_V A_V(\tau_V)
\end{align*}
\]

where for each particle \(p = S, f, V\), \(\tau_p = m_p^2/4m_h^2\), \(N_p\) is the number of colors, \(C_p^2\) is the Casimir of the color representation \((\text{Tr}(T^a T^b) = C_p^2 \delta^{ab})\), and the loop functions are

\[
\begin{align*}
    A_{\gamma S}(\tau) &= \frac{3}{\tau^2} [f(\tau) - \tau] , \\
    A_f(\tau) &= \frac{3}{2\tau^2} [(\tau - 1) f(\tau) + \tau] \\
    A_V(\tau) &= \frac{1}{\tau^2} [3(2\tau - 1) f(\tau) + 3\tau + 2\tau^2]
\end{align*}
\]

with \(f(\tau) = \arcsin^2(\sqrt{\tau})\) for \(\tau \leq 1\) such that \(A_p(\tau_p) \to 1\) in the limit \(\tau_p \to 0\) (heavy \(p\)-particle).

In particular, in the SM, the \(hgg\) coupling is dominated by the top loop, and the \(h\gamma\gamma\) coupling arise from the sum of the top and \(W\) boson loops:

\[
\begin{align*}
    c_{gg}^{SM} = c_\gamma^{(t)} &= A_f(\tau_t) &
    c_{\gamma\gamma}^{SM} &= c_\gamma^{(t)} + c_\gamma^{(W)} = \frac{2}{9} A_f(\tau_t) - \frac{7}{8} A_V(\tau_W) .
\end{align*}
\]

Beyond the SM (BSM) physics affects the parameters \(r_g\) and \(r_\gamma\) as

\[
\begin{align*}
    r_g &= 1 + \frac{c_{gg}^{BSM}}{c_{gg}^{SM}}, &
    r_\gamma &= 1 + \frac{c_{\gamma\gamma}^{BSM}}{c_{\gamma\gamma}^{SM}} .
\end{align*}
\]

For example, additional scalar particles with the same quantum numbers of a stop, sbottom and stau respectively contribute to \(c_{gg}^{BSM}\) and to \(c_{\gamma\gamma}^{BSM}\) as:

\[
\begin{align*}
    c_\gamma^{(t)} &= \frac{1}{4} r_{\tau_t} A_{\gamma S}(\tau_t) &
    c_\gamma^{(b)} &= \frac{1}{4} r_{\tau_b} A_{\gamma S}(\tau_b) &
    c_\gamma^{(\tau)} &= 0 \\
    c_\gamma^{(t)} &= \frac{1}{15} r_{\tau_t} A_{\gamma S}(\tau_t) &
    c_\gamma^{(b)} &= \frac{1}{72} r_{\tau_b} A_{\gamma S}(\tau_b) &
    c_\gamma^{(\tau)} &= \frac{1}{24} r_{\tau_\tau} A_{\gamma S}(\tau_\tau).
\end{align*}
\]

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